



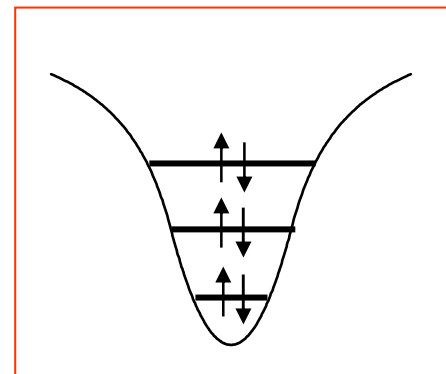
## Photoelectron spectroscopy on simple metal clusters

B.v.Issendorff

What is the correct description of a simple metal nanoparticle?



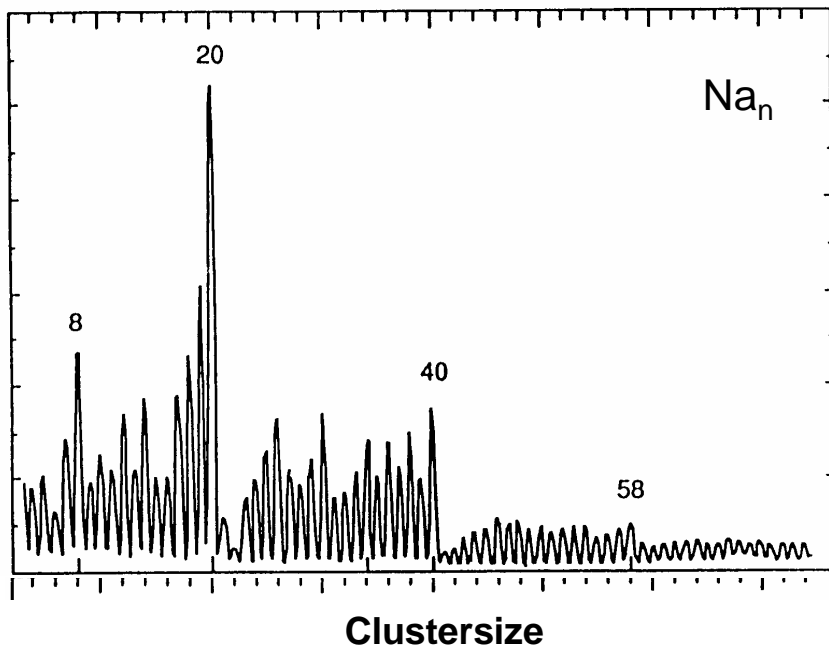
High or low symmetry  
Supermolecule



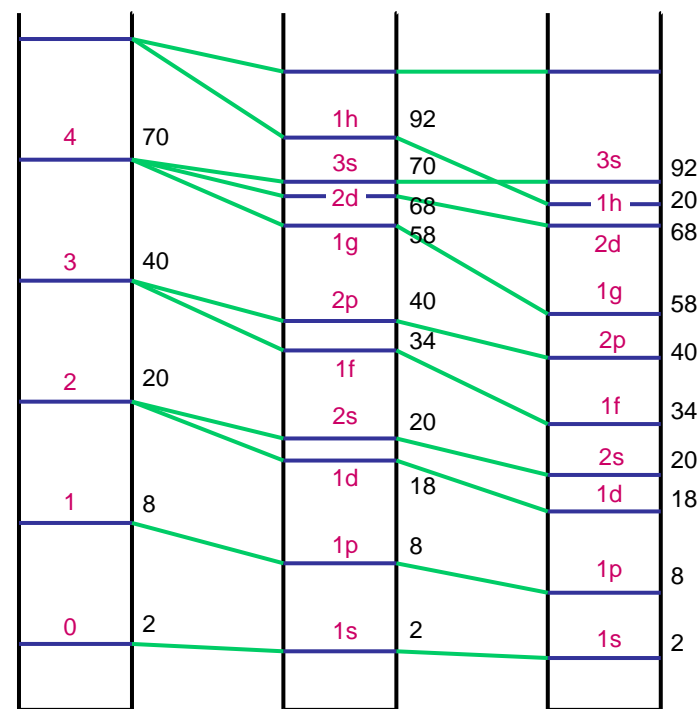
Trapped Fermi gas  
(parabolic trap filled  
with electrons)



# Electron shells: spherical box model



Knight, de Heer, 1984



Harmonic Oscillator

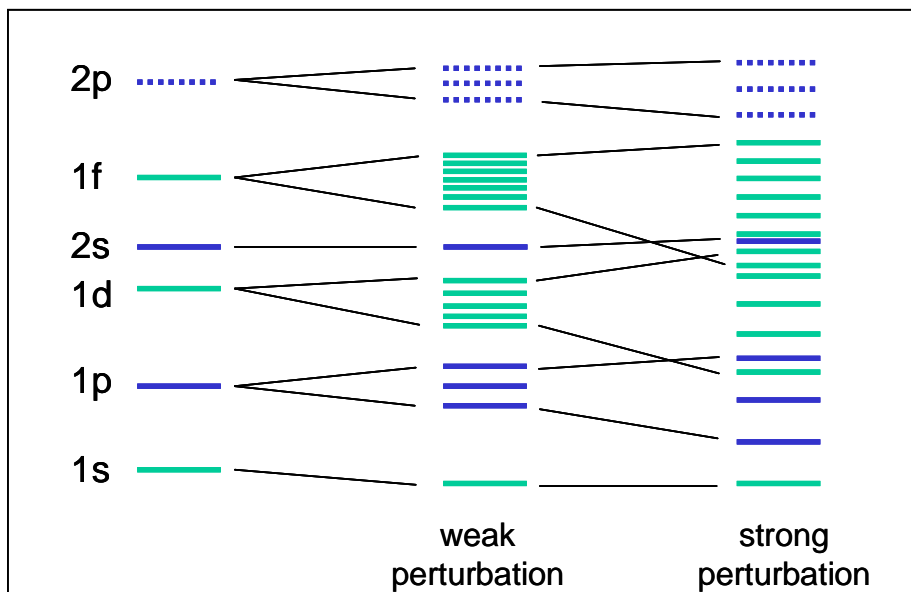
Woods Saxon

Box-Potential

Electron levels in different spherical model potentials



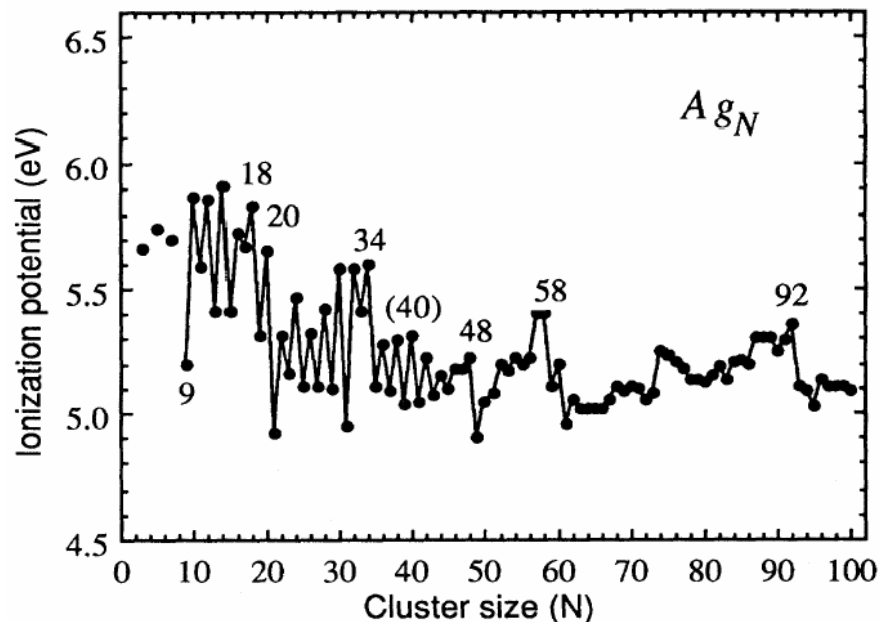
# Shell structure in a real cluster



The atomic structure  
perturbs the electron angular  
momentum eigenstates

**Ideal probe: Photoelectron-spectroscopy  
(Lineberger, Bowen, Smalley, Cheshnovsky,  
Meiwes-Broer...)**

Ionization potentials of silver clusters:  
evidence for perturbed shell structure



Alameddin et al.  
Chem.Phys. Lett. 192, 122 (1992)



# Program

## Experiment

**Photoelectron spectroscopy  
cluster thermalization**

## Sodium clusters

**Electronic shell structure  
Interaction with geometric structure  
Cluster shapes: comparison to simple models  
Structure of larger clusters  
Comparison with potassium clusters**

## Noble metal clusters

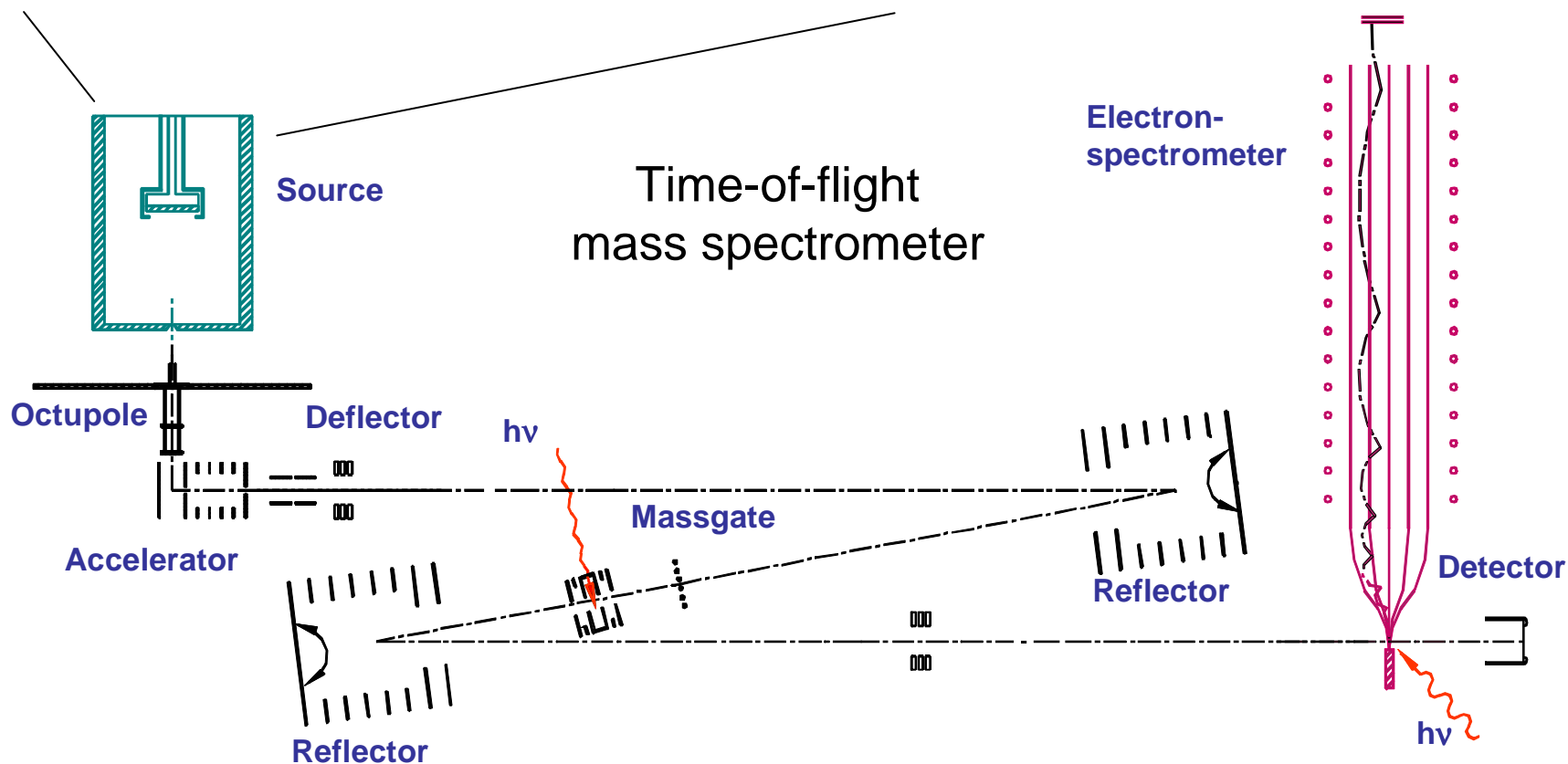
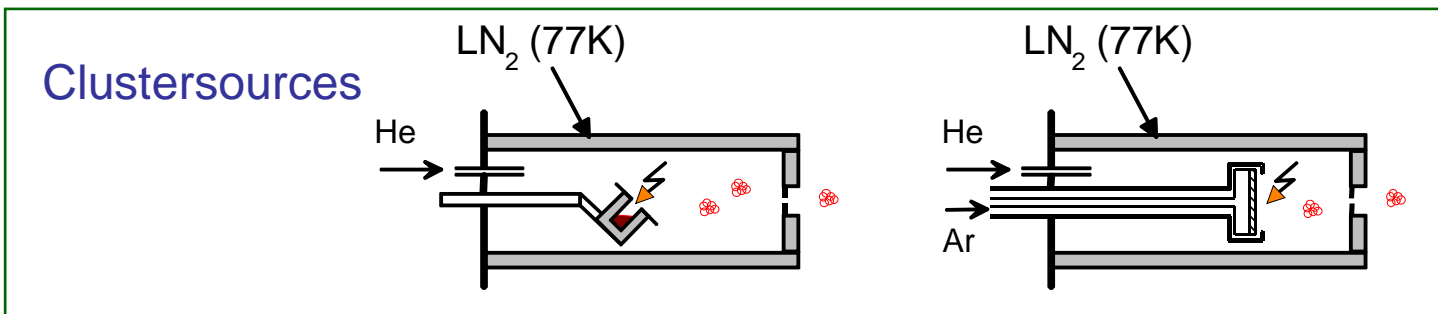
**Electronic structure  
Geometrical structure  
special case: gold clusters  
Comparison Na, Cu, Ag, Au**

## Angle resolved photoelectron spectroscopy

**Basics  
Results on Na, Ag, Cu**

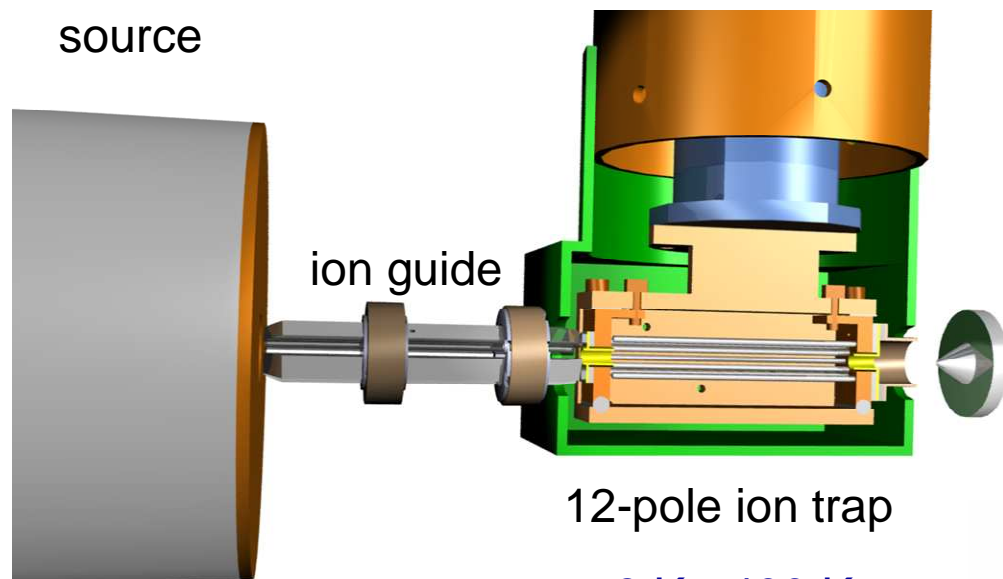


# Experiment





# Cluster Thermalization



ion guide

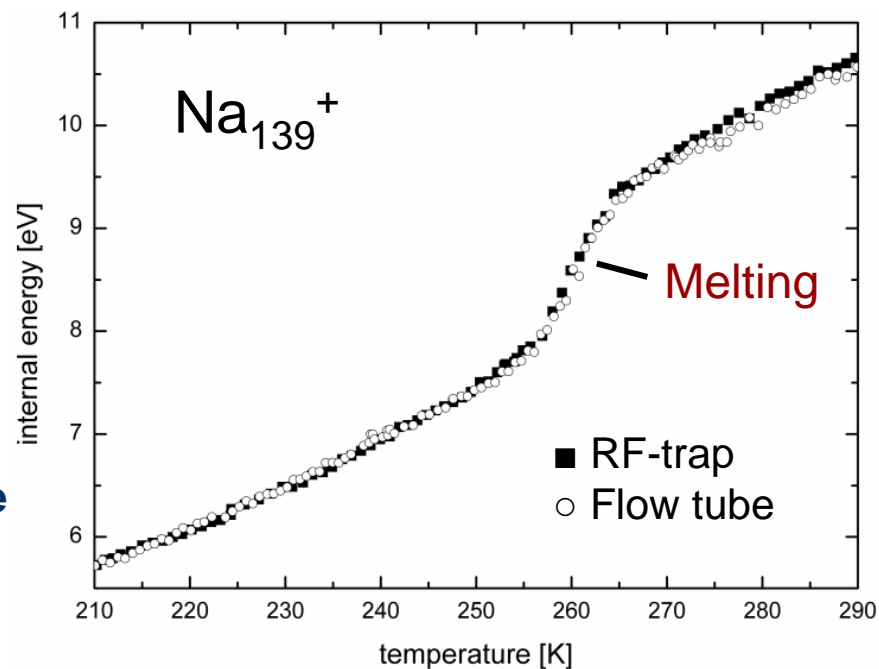
12-pole ion trap

6 K - 400 K

Check of temperature:  
Comparison with flow tube  
thermalization

Linear RF-Trap for cluster  
thermalization after production

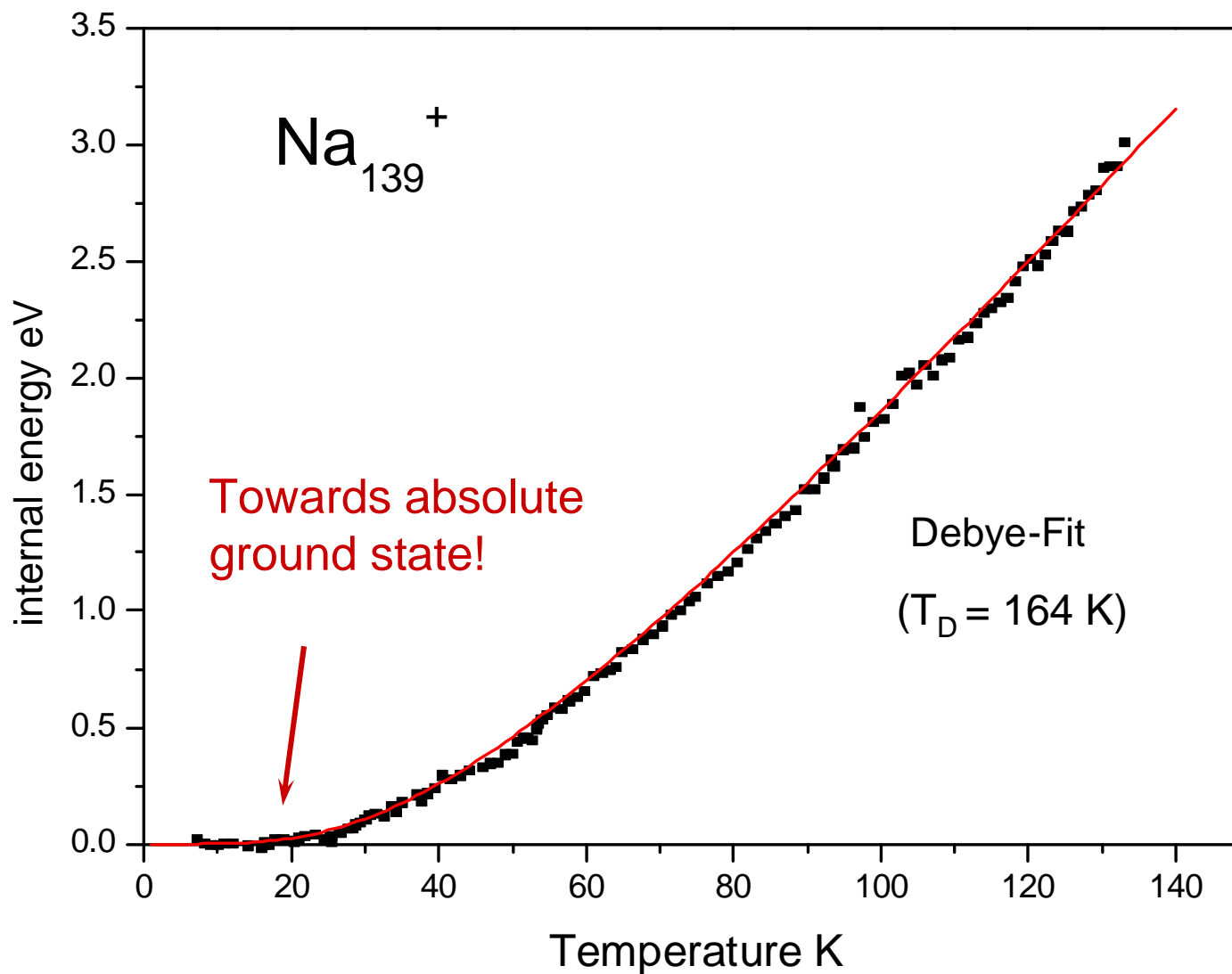
Caloric Curve





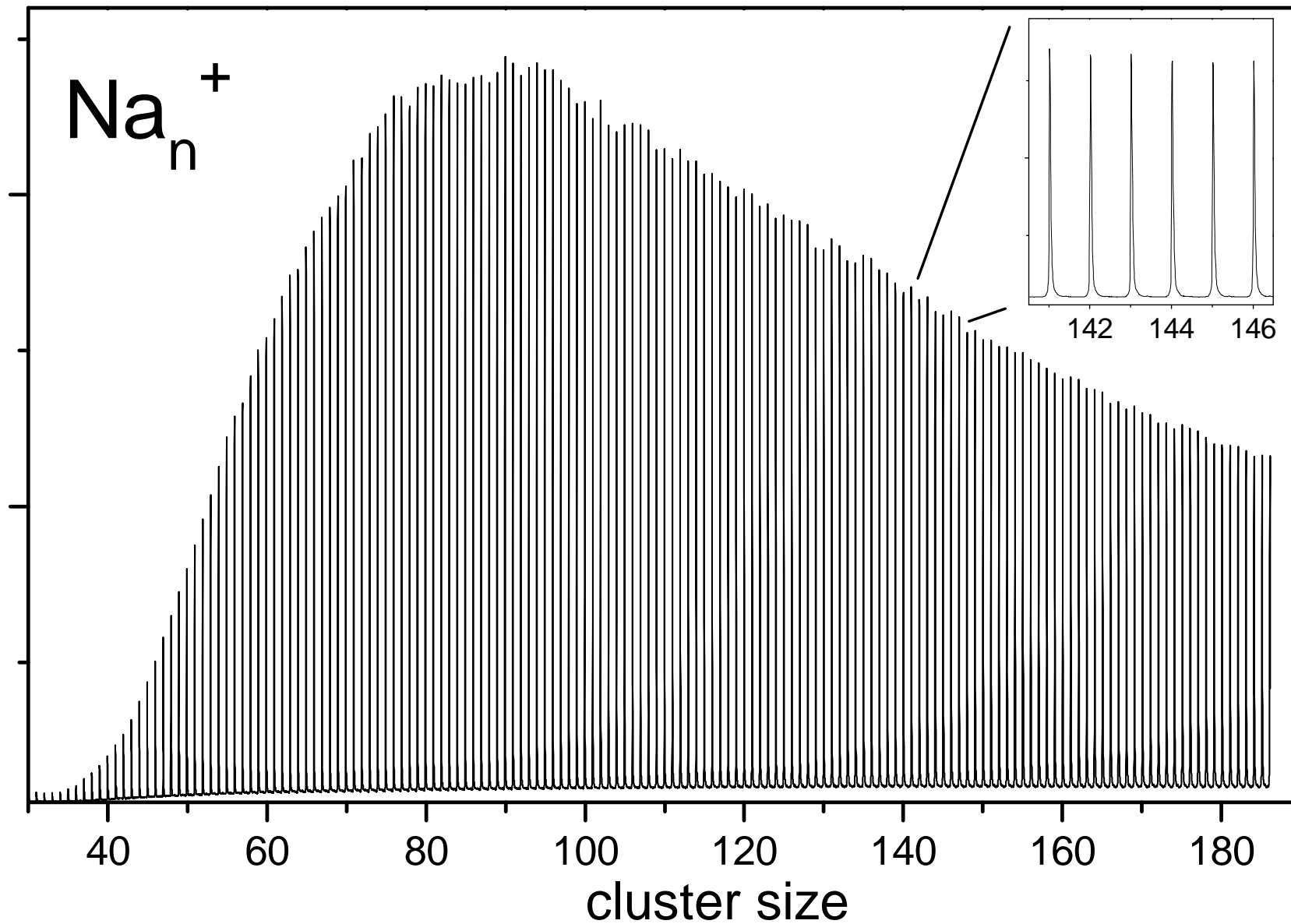
# Very low temperatures

Caloric curve of clusters thermalized in RF-Trap





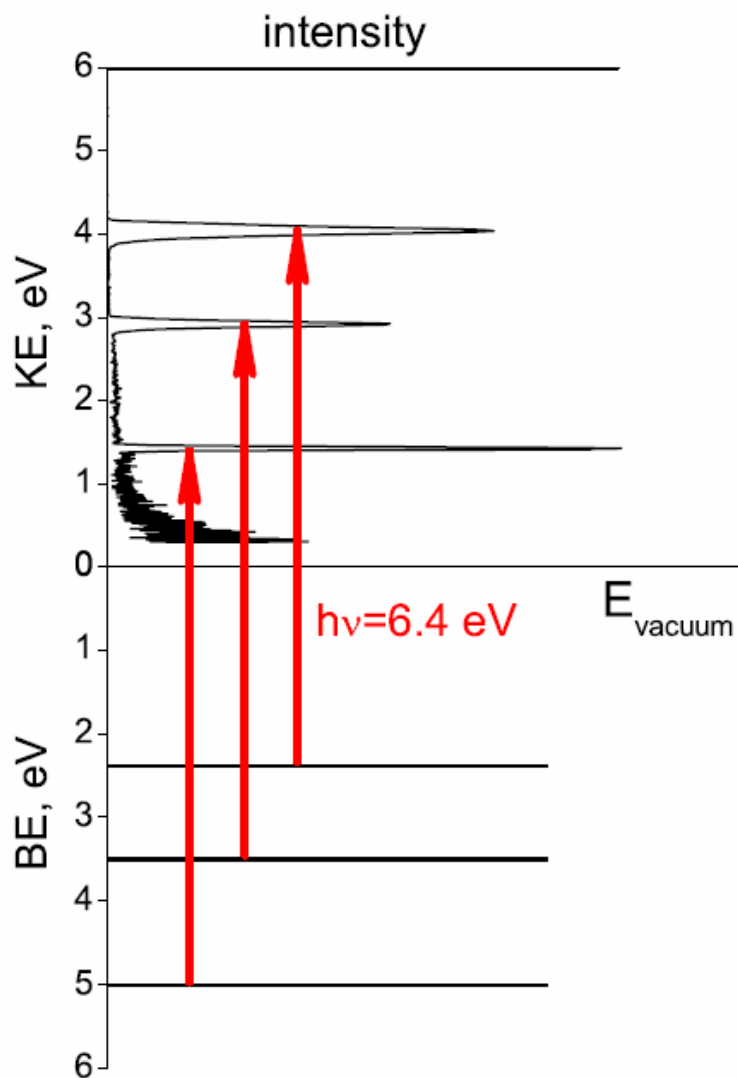
# Mass spectrum of sodium clusters







# Photoelectron spectroscopy: principle



**Photoeffect:**

$$E_{kin} = h\nu - E_{bin}$$

**broadening effects:**

- vibrational (de)excitation
- hole lifetime

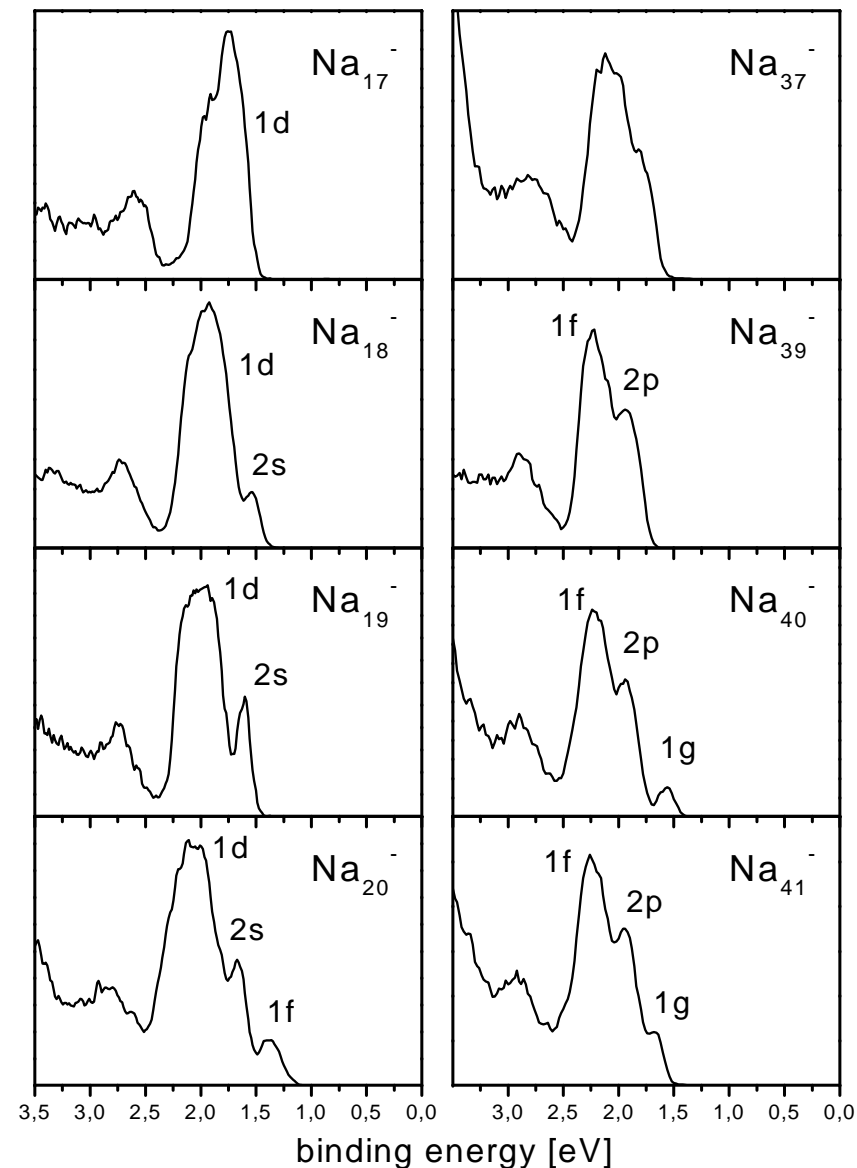


# PES on hot sodium clusters

Jellium levels:

1s	1p	1d	2s	1f	2p	1g
2	8	18	<u>20</u>	34	<u>40</u>	<u>58</u>

ideal electron shell structure!

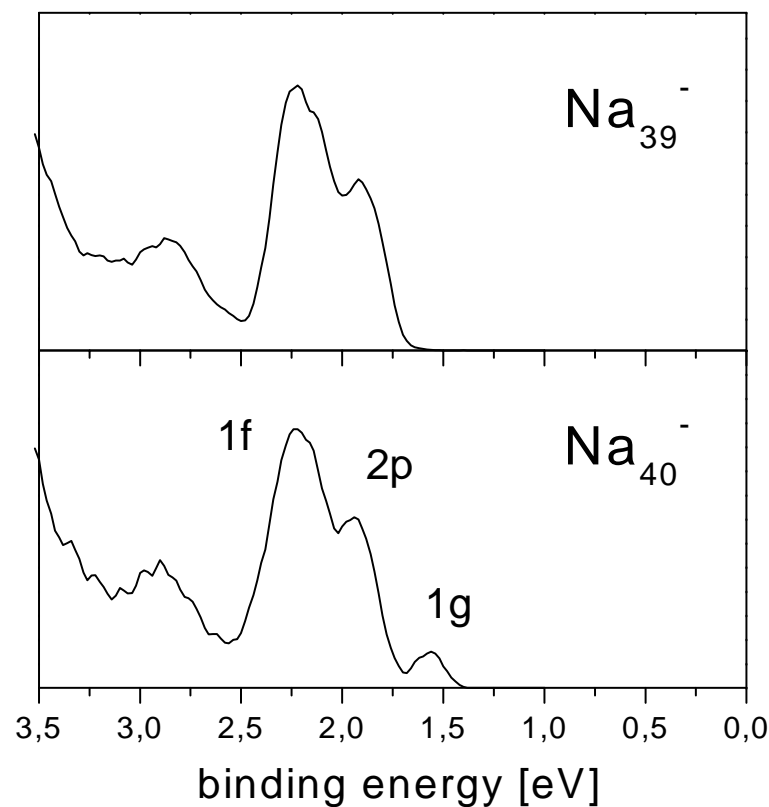




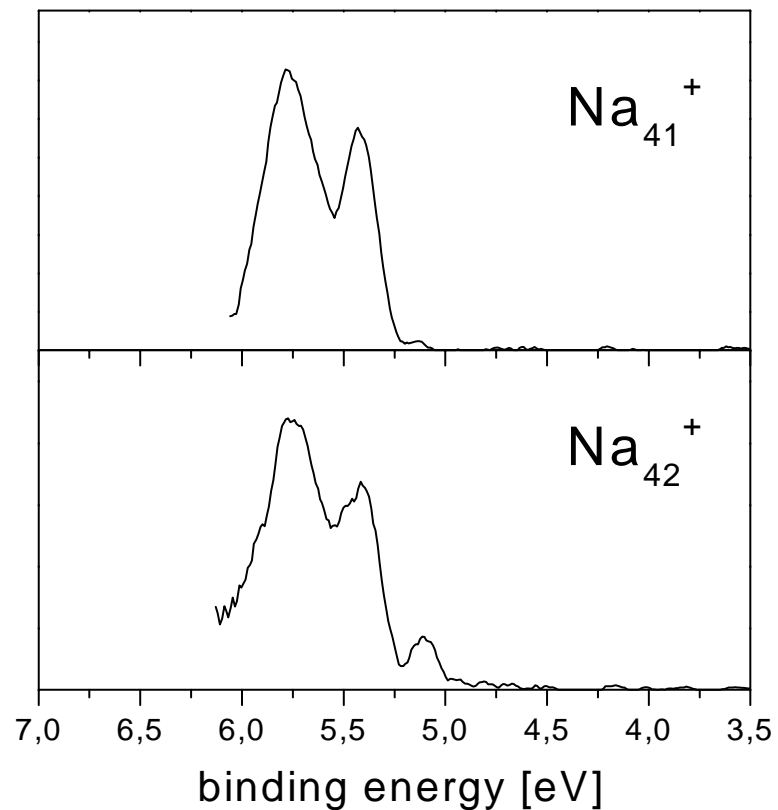
# Comparison of cluster anions and cations

negative

positive



40 e<sup>-</sup>



41 e<sup>-</sup>

Identical DOS despite different geometrical structures!

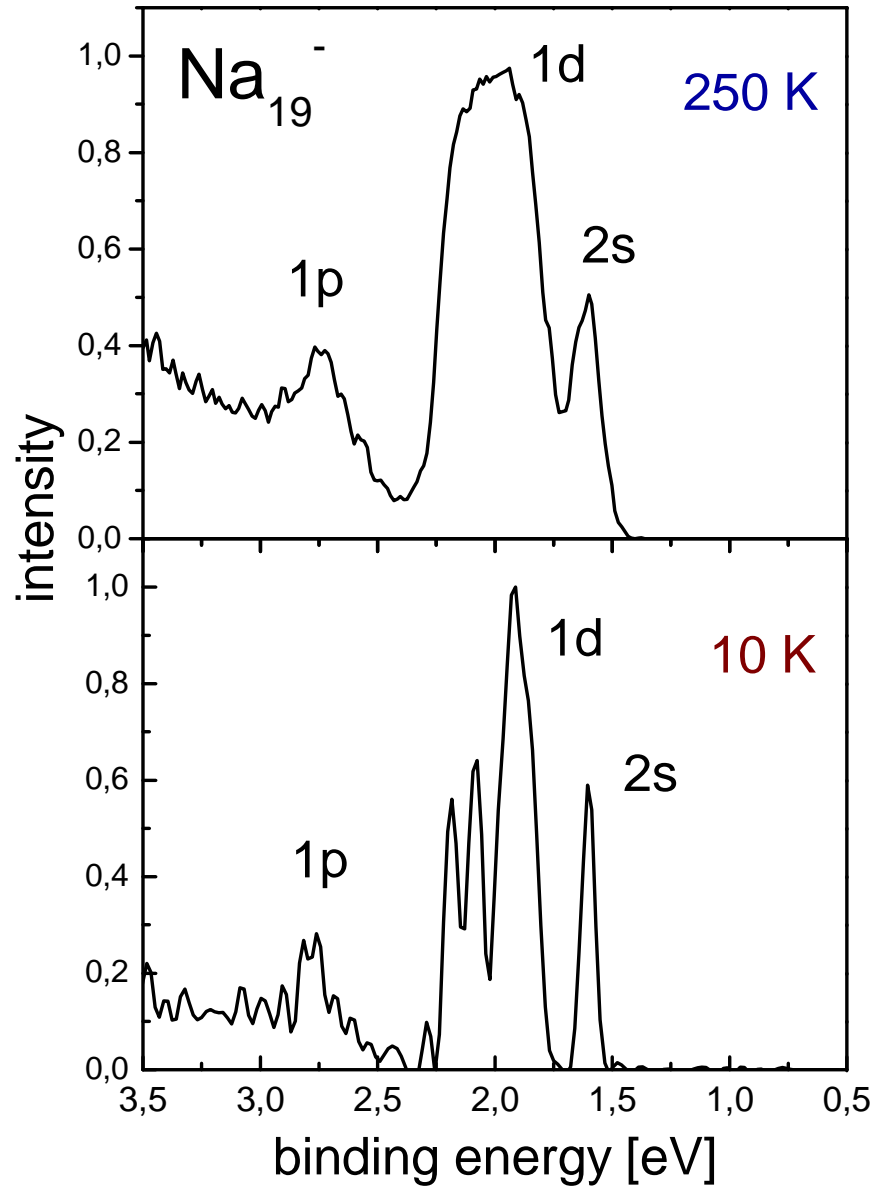


# Temperature dependence of PES

20 valence electrons:  
spherical shape

Strong splitting  
of d-state:

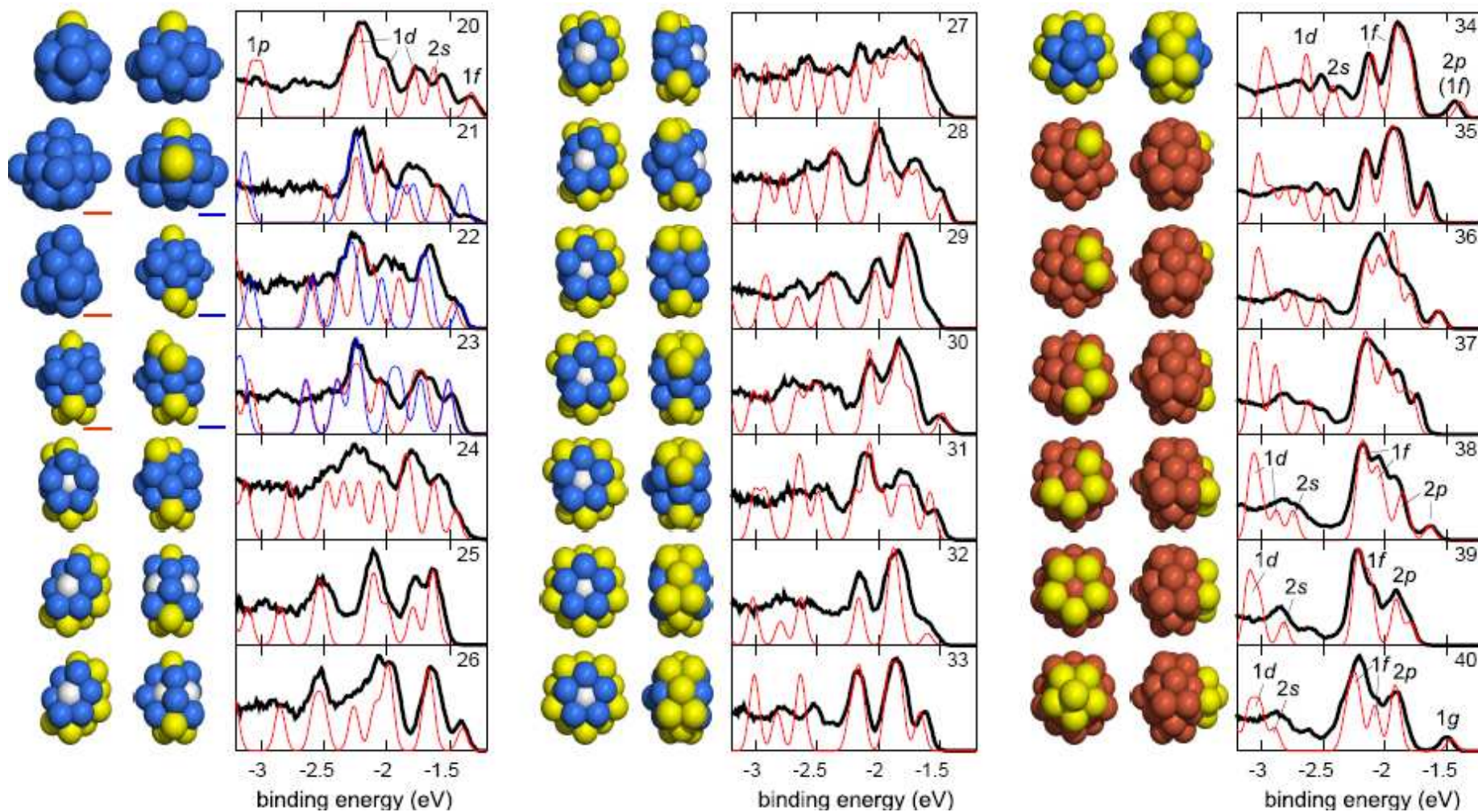
electron-lattice  
interaction!





# PES of $\text{Na}_n^-$ : $n = 20-40$

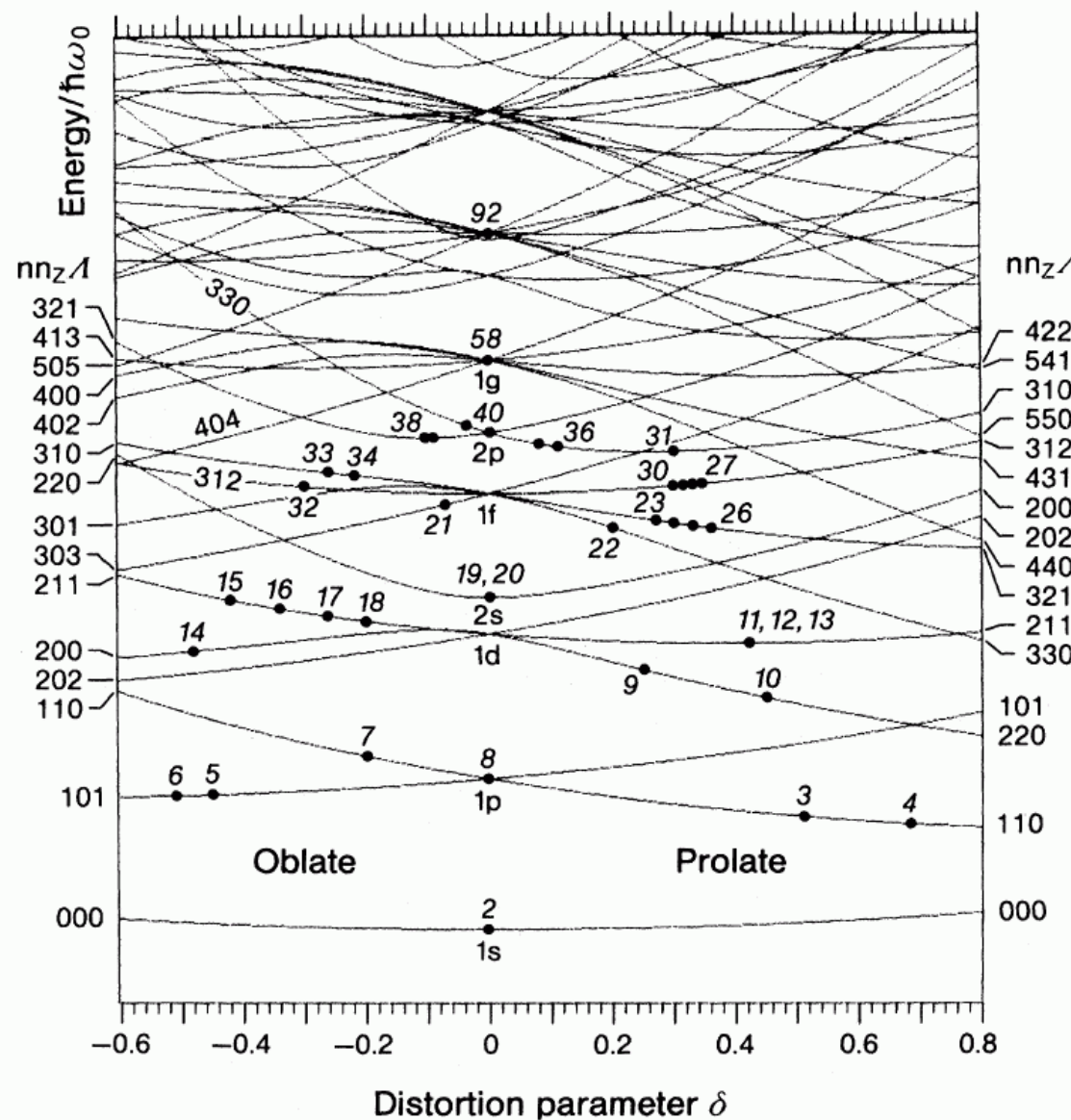
$T = 100 \text{ K}$



DFT- calculations by  
M. Moseler and B. Huber



# Cluster deformation: Clemenger-Nilsson-model



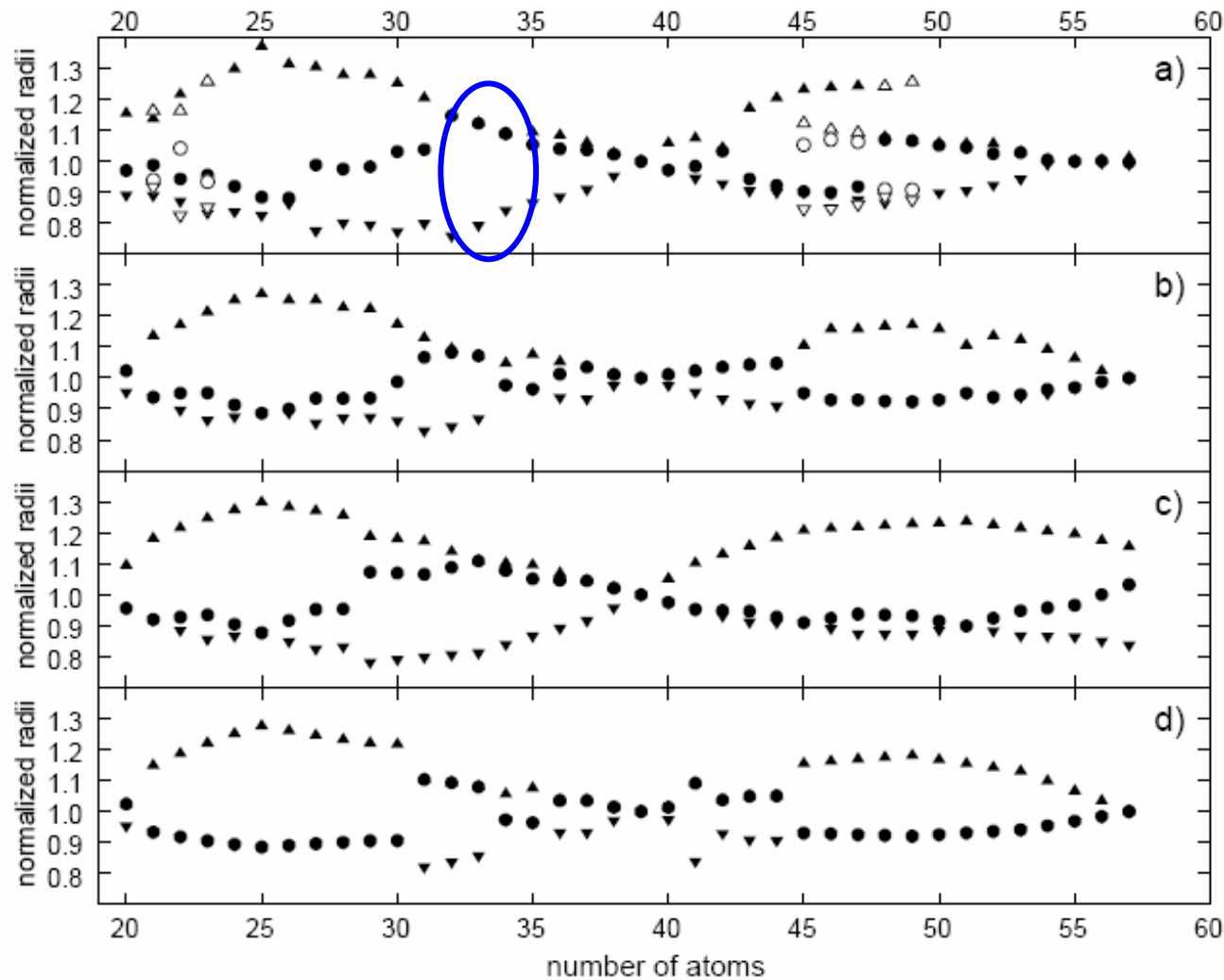
Spherical shape  
only for closed shell  
sizes  
(electron numbers  
8, 20, 40, 58, 92..)



# Deformation: comparison to simple models

Radii as derived from moment of inertia

34 electrons: closed shell!



Experiment  
+ DFT

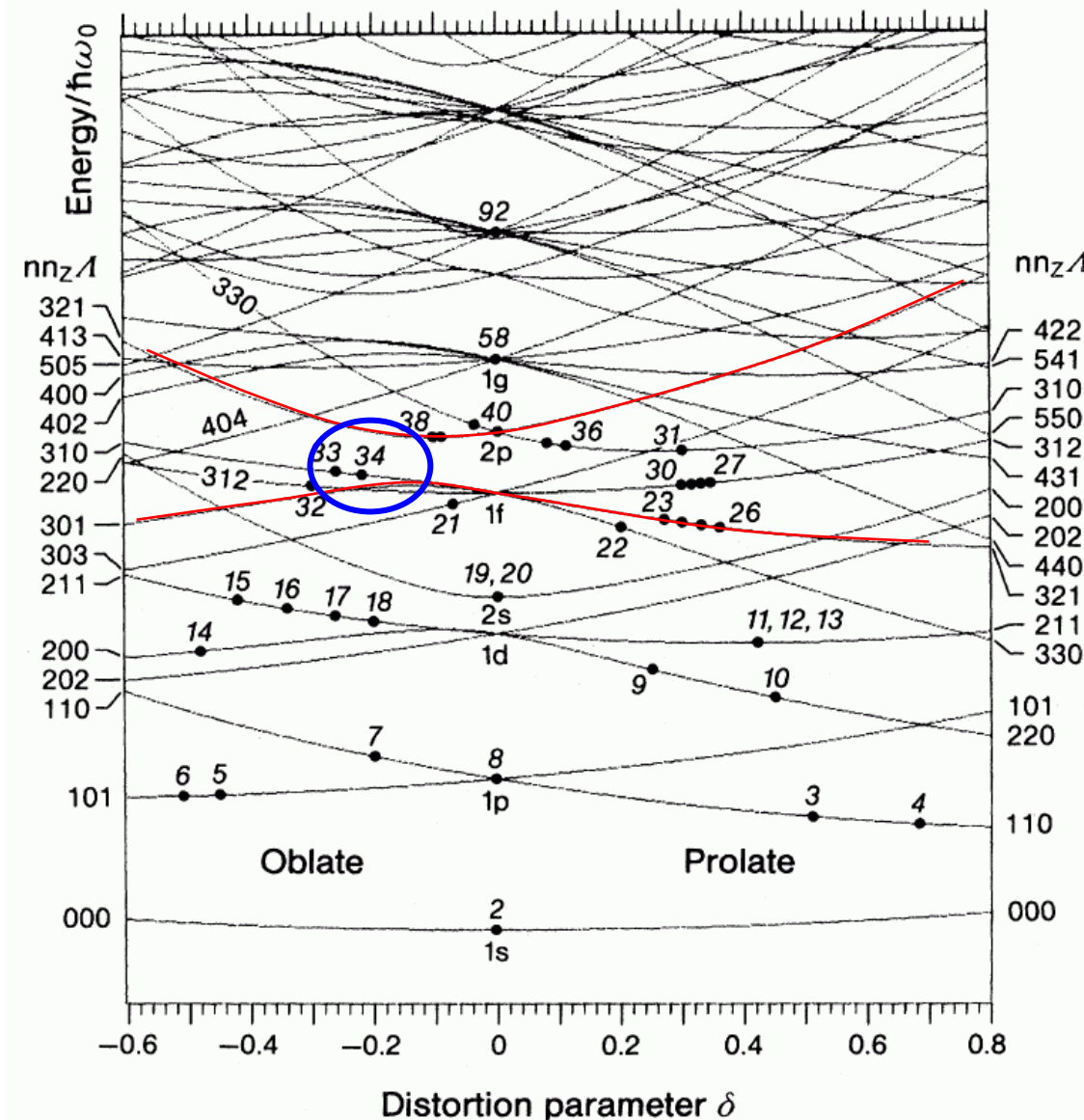
Triaxial  
Jellium

Triaxial  
harmonic  
Oscillator

Clemenger/  
Nilsson



# Deformation: avoided crossings



Clemenger-Nilsson-model

Quadrupole deformation:

**Perturbing potential**

$$V(r, \theta, \varphi) = f(r) Y_{20}(\theta, \varphi)$$

⇒ mixing of states  
with  $\Delta l=2$

⇒ avoided crossing  
between 1f and 2p

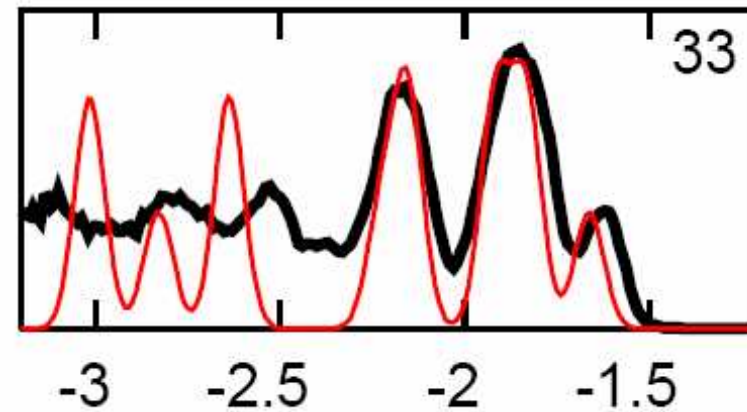
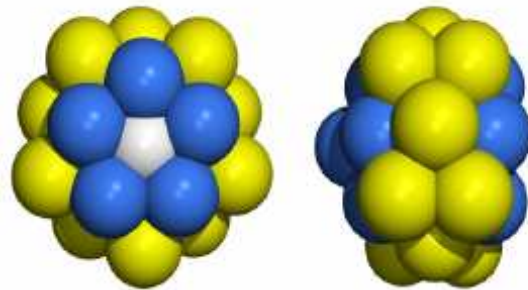
⇒ stabilization of  
deformation



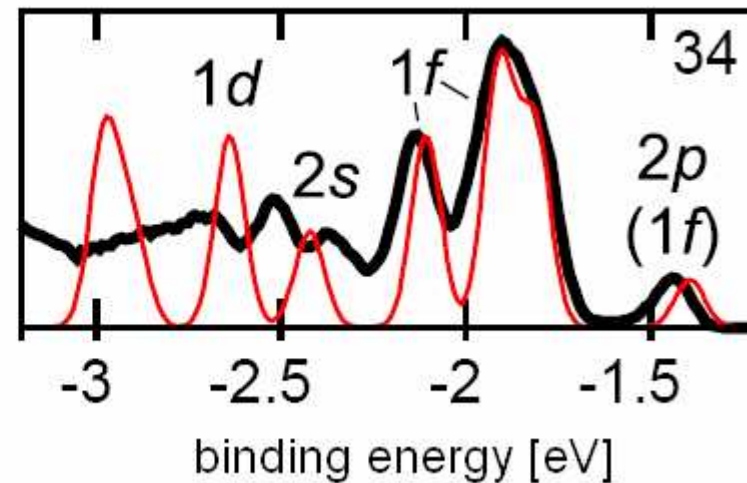
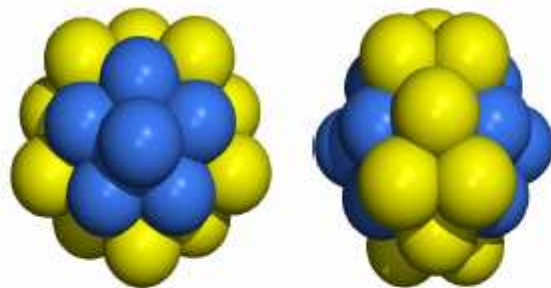


# Deformation: the 34 electron case

**Prolate (quadrupole) deformation: mixing between 1f and 2 p stabilizes nonspherical shape of closed shell structure**



Oblate!



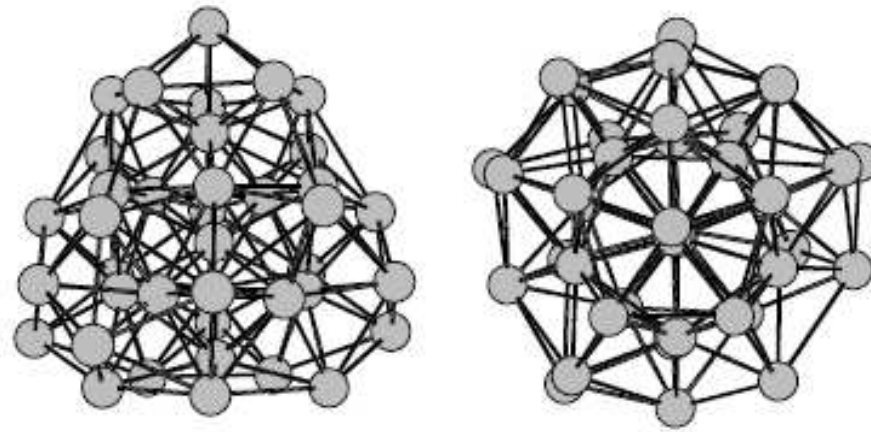


# Deformation: the 40 electron case

Octupole deformation mixes  
2p and 1g ( $\Delta l=3$ ):

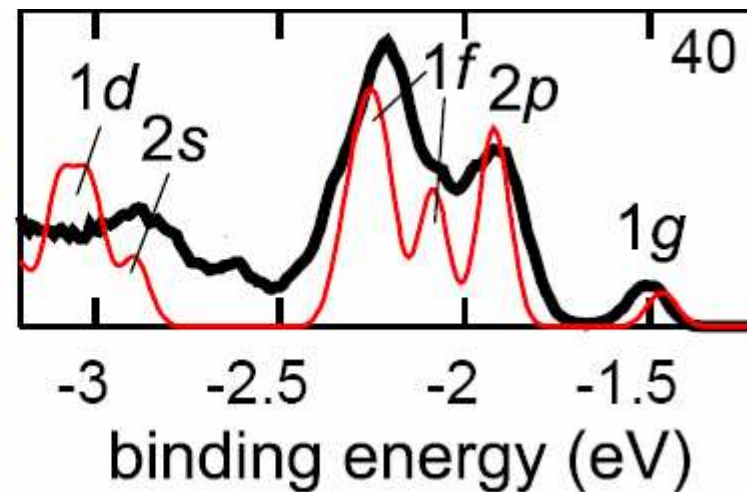
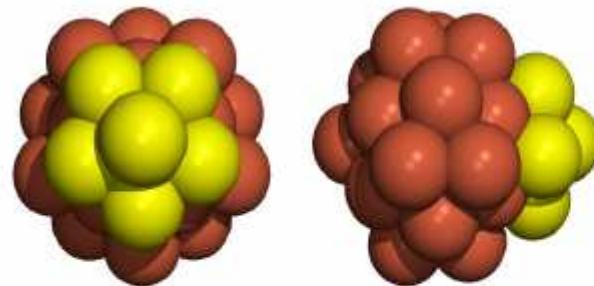
Stabilization of deformation

## Simulated structure of hot $\text{Na}_{40}$



A.Rytkönen et al., PRL 80, 3940 (1998)

## Experiment/DFT





# Program

Experiment

Photoelectron spectroscopy  
cluster thermalization

Sodium clusters

Electronic shell structure  
Interaction with geometric structure  
Cluster shapes: comparison to simple models  
**Structure of larger clusters**  
**Comparison with potassium clusters**

Noble metal clusters

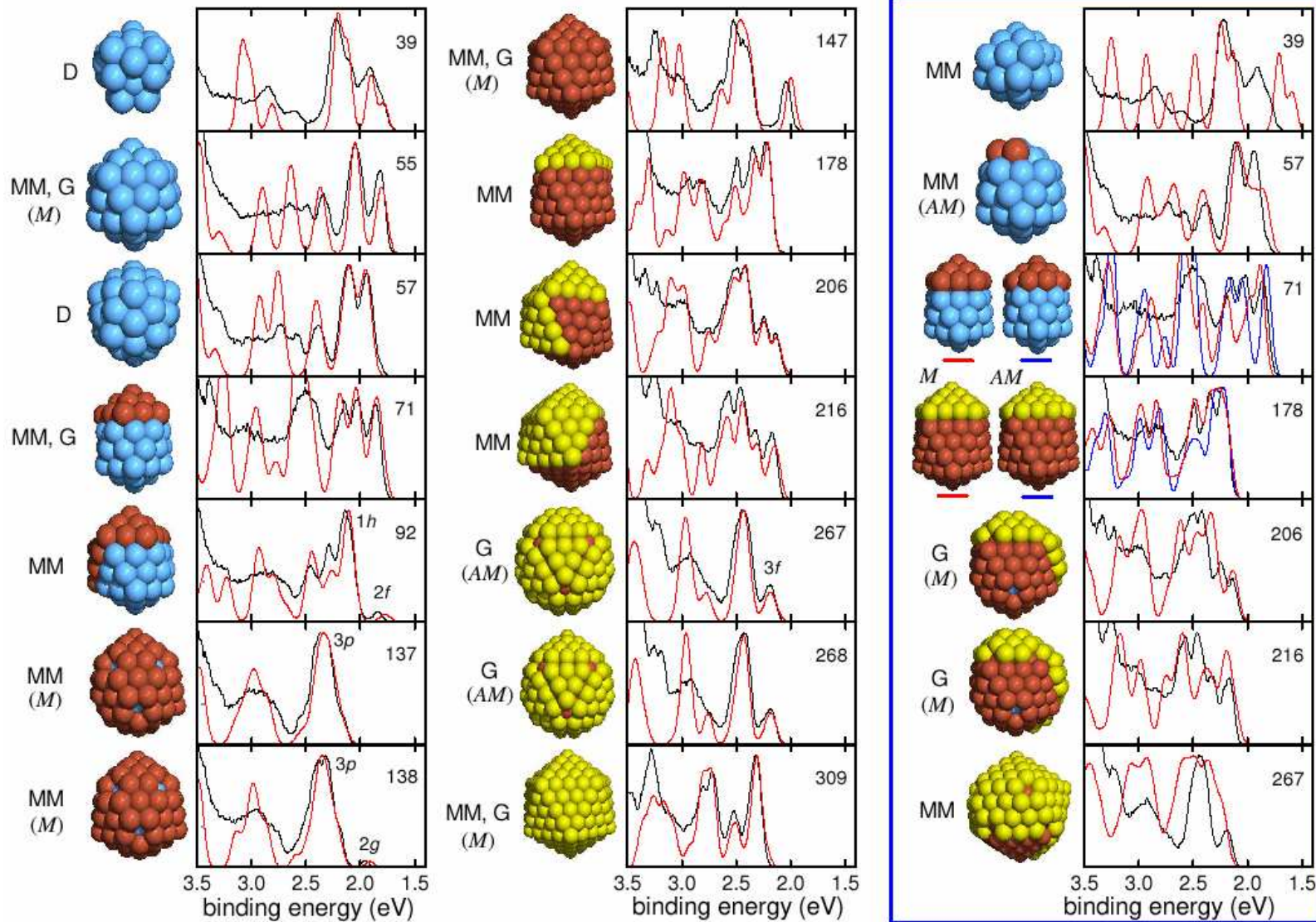
Electronic structure  
Geometrical structure  
special case: gold clusters  
Comparison Na, Cu, Ag, Au

Angle resolved photoelectron spectroscopy

Basics  
Results on Na, Ag, Cu

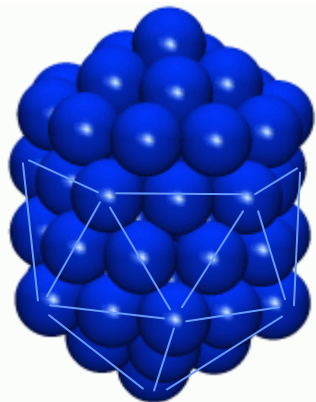


# PES of $\text{Na}_n^-$ : $n = 39-309$

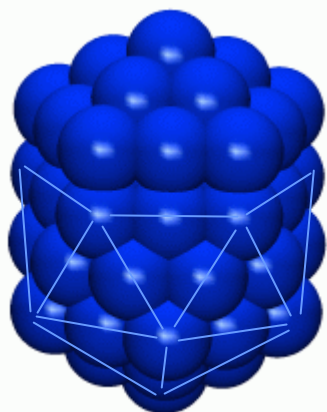




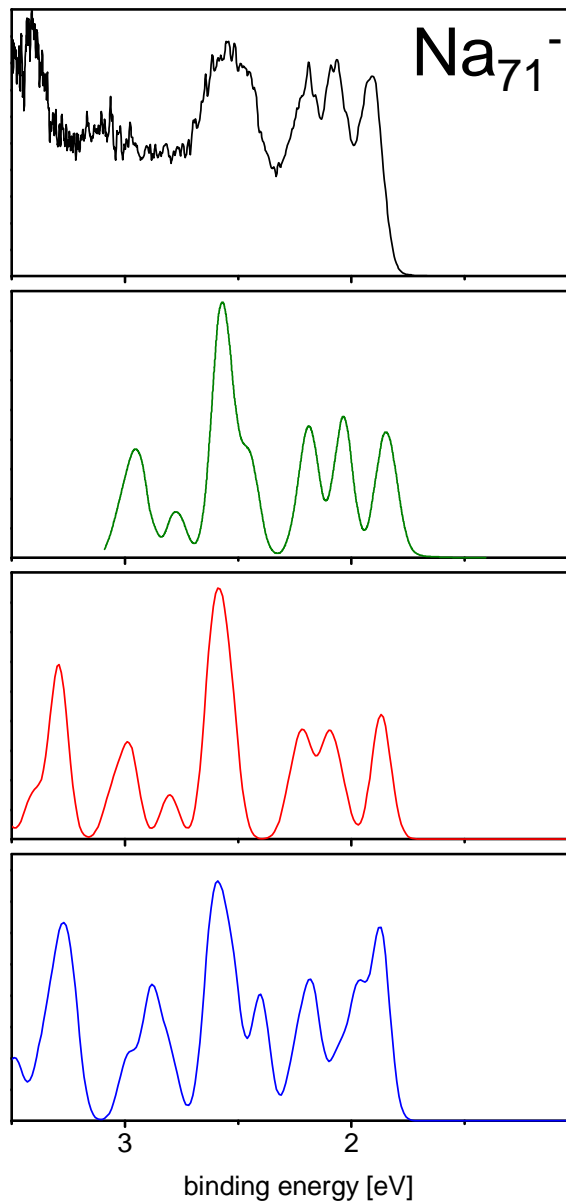
# Sodium: Mackay / anti-Mackay stacking



55 atom icosahedron with anti-Mackay-cap



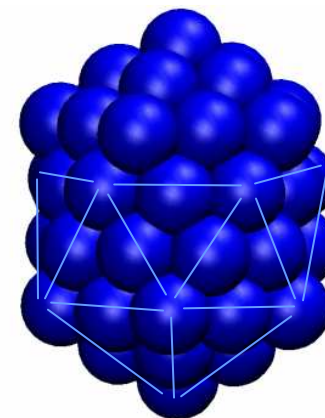
55 atom icosahedron with Mackay-cap



Experiment

Calculated DOS

(M.Moseler, IWM Freiburg)

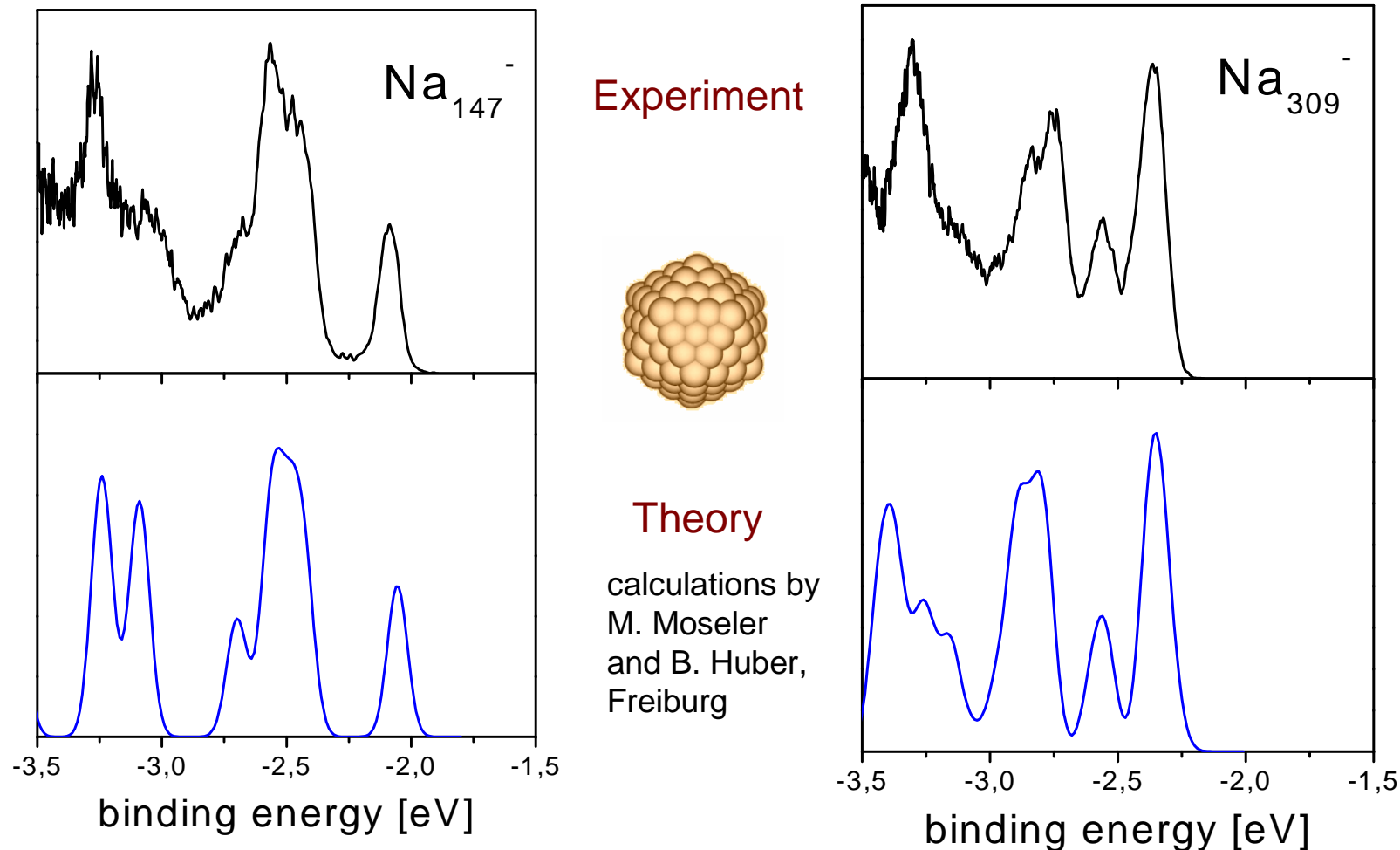


55 atom icosahedron with twisted cap

(Noya et al., EPJD 43, 57 (2007))



# Comparison with theory

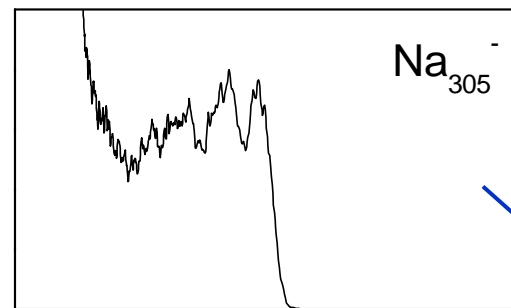
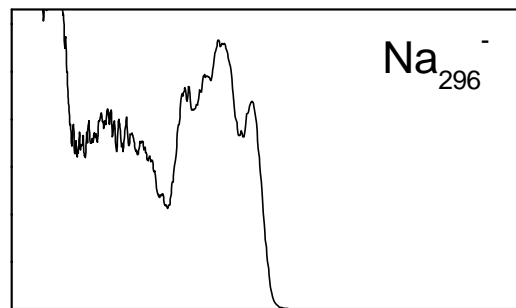


Closed shell icosahedral structures!



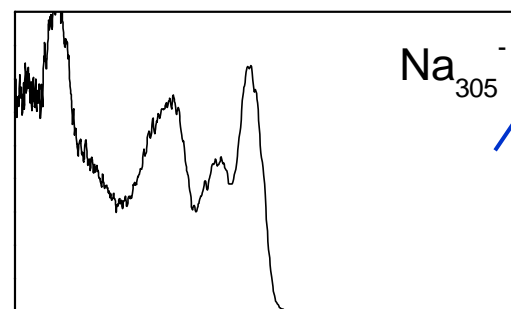
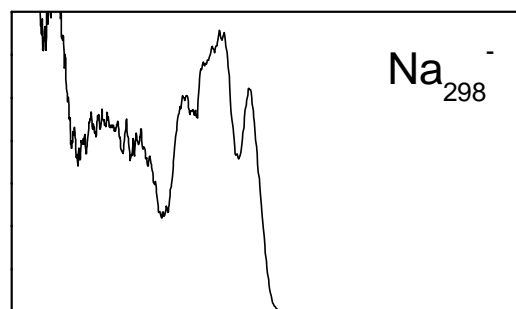
# Abrupt structure change at size 305

Unknown  
Structure!

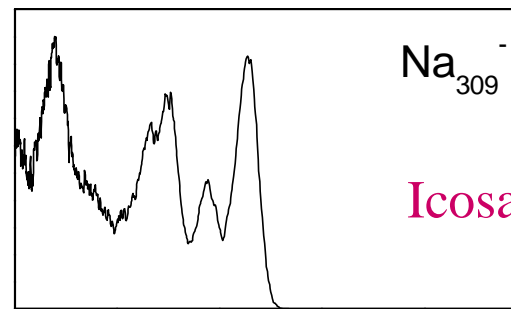
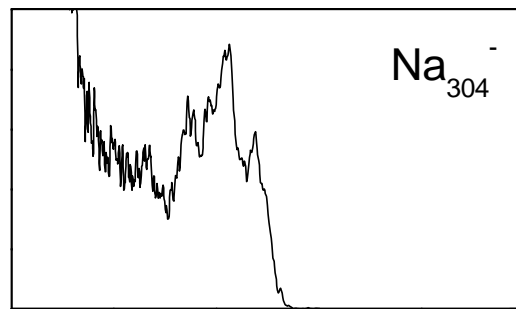


T=150 K

Same  
size!



T=100 K



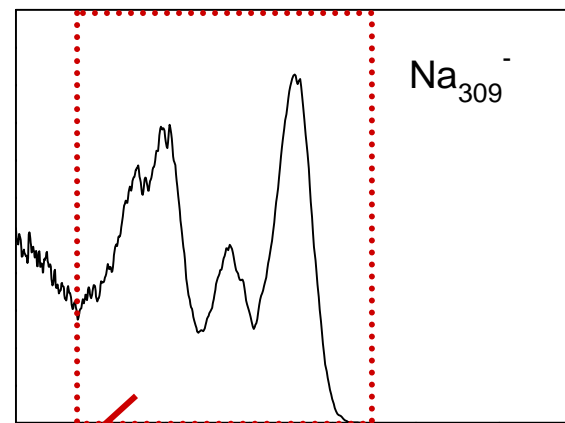
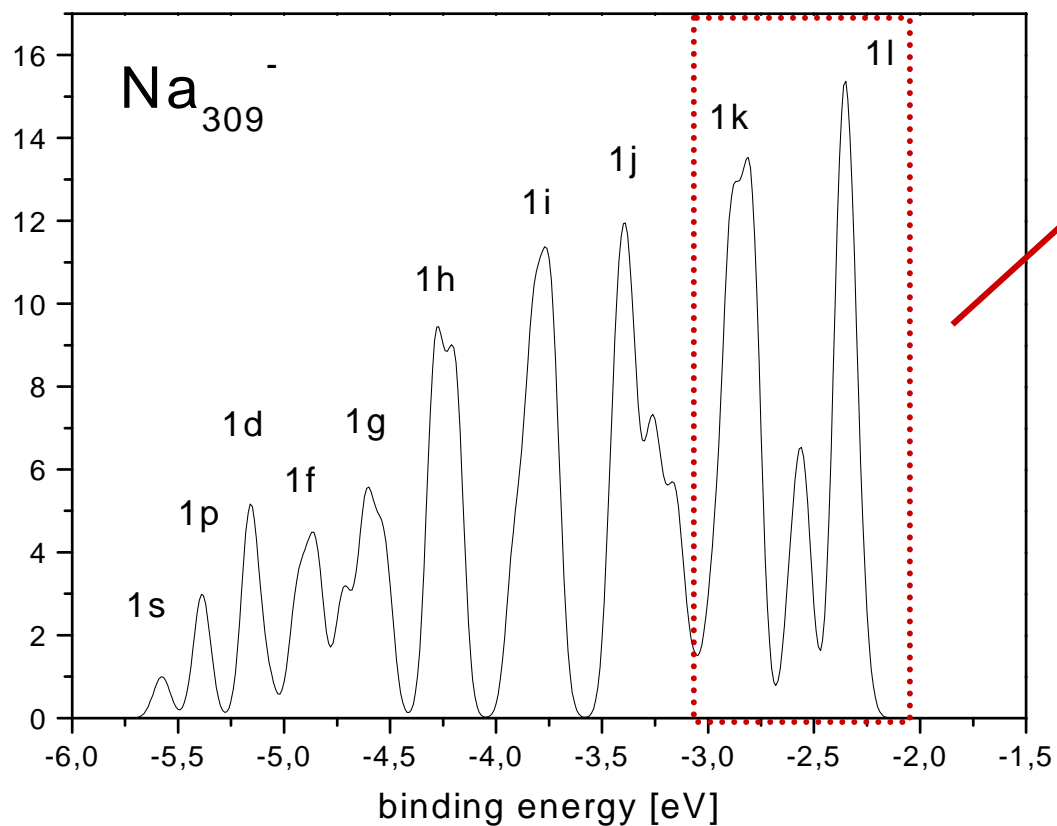
Icosahedron

binding energy [eV]



# Electron shell structure in a large cluster

Total calculated DOS of the icosahedral cluster



measured  
photoelectron  
spectrum

DFT- calculations by  
M. Moseler  
and B. Huber,  
Freiburg

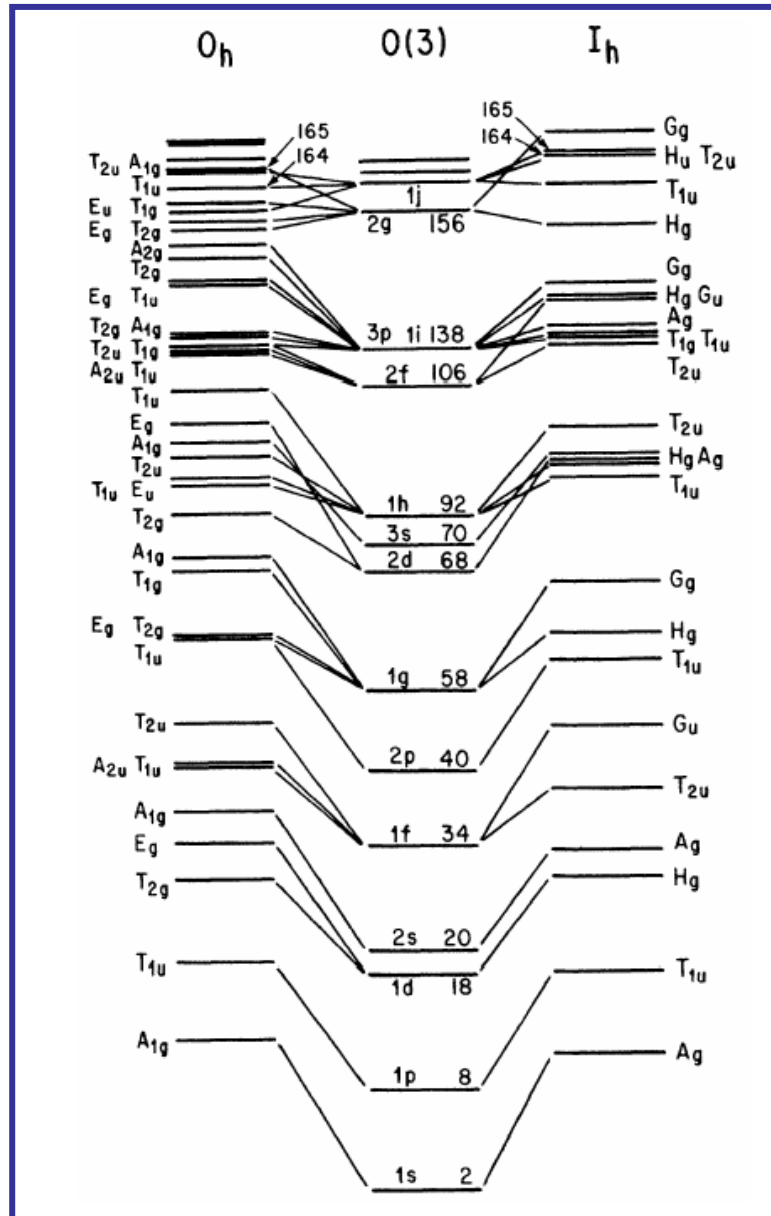




# Crystal field splitting in clusters

Splitting of angular momentum eigenstates

octahedral symmetry



icosahedral symmetry

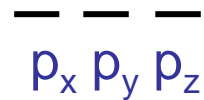
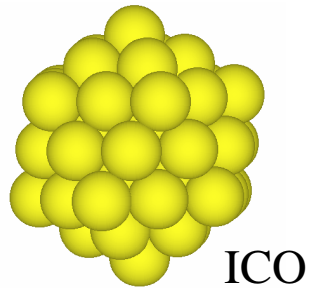
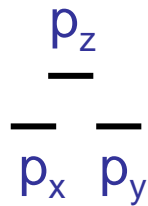
higher degeneracy!



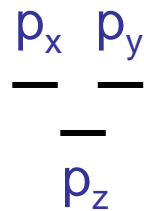
# Symmetry perturbation

2p-shell

minus 2 atoms:  
oblate

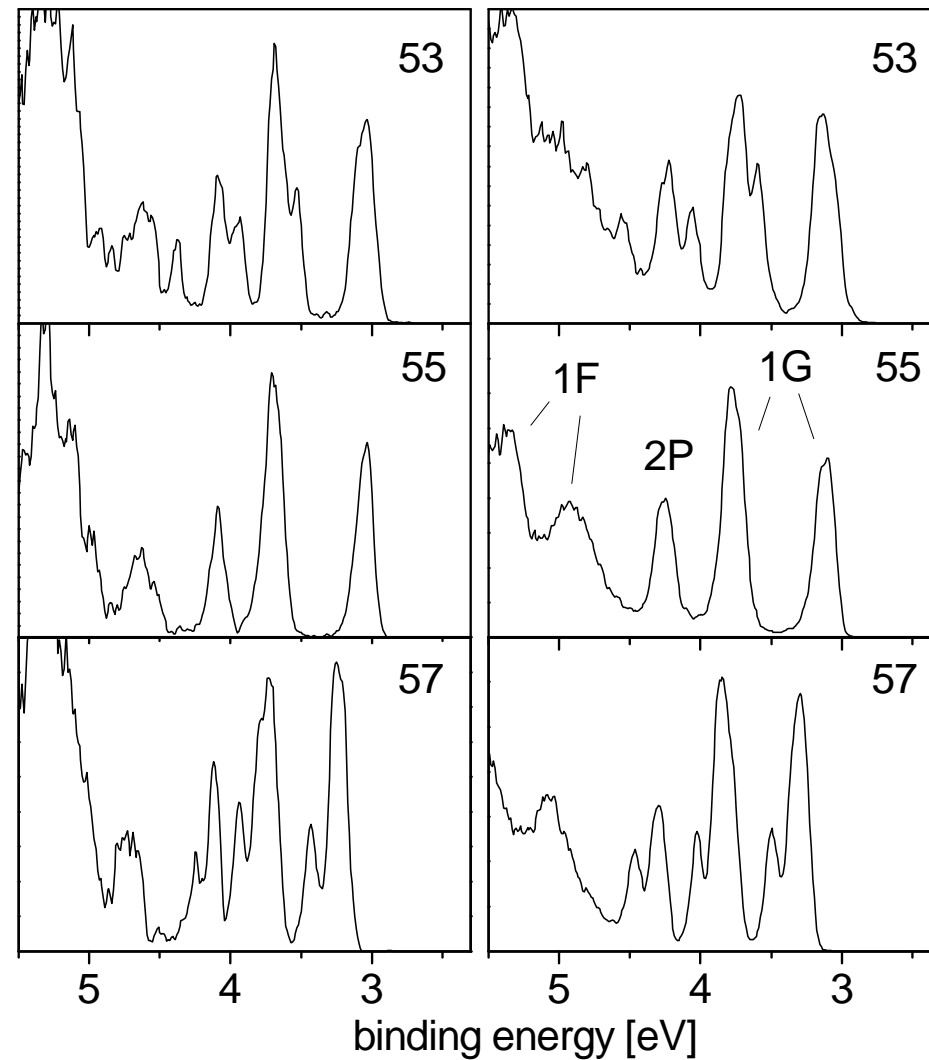


plus 2 atoms:  
prolate



Cu

Ag



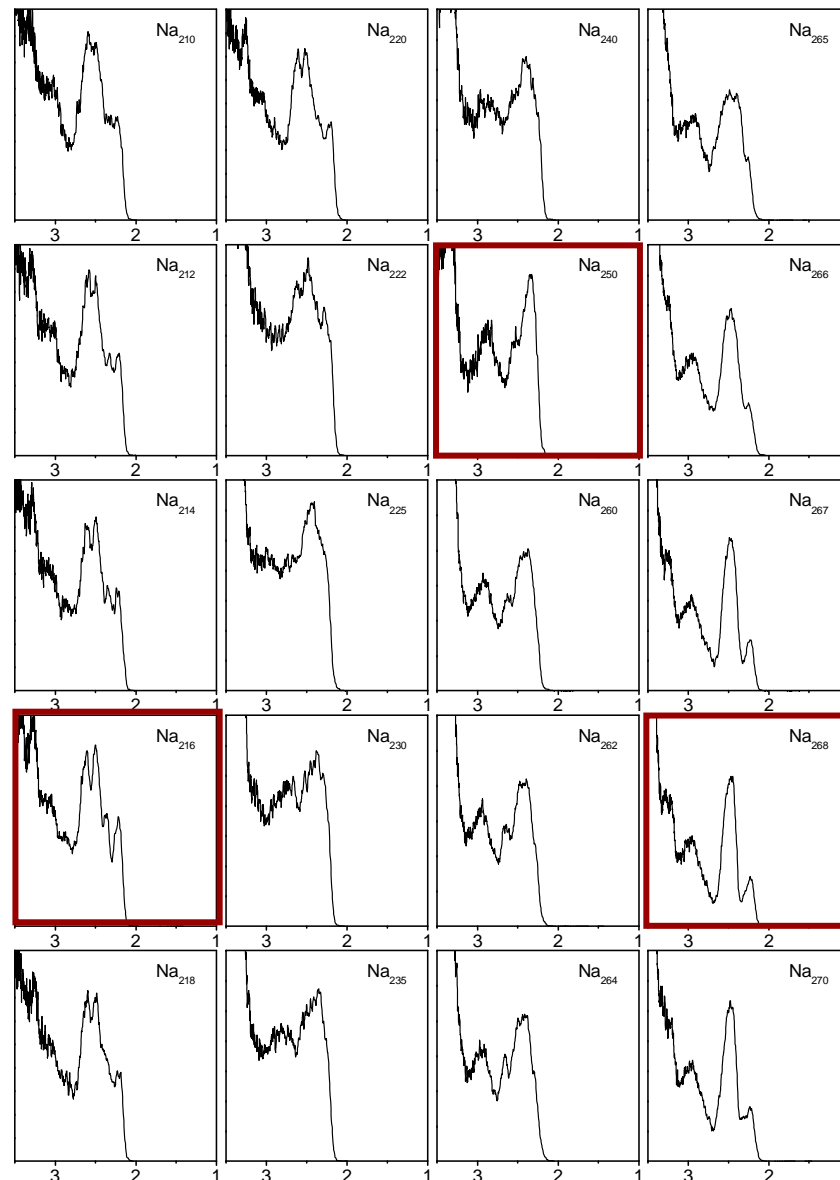


# Size dependence of spectra

Spectra of  $\text{Na}_n^-$  with  
 $n=210-270$ :

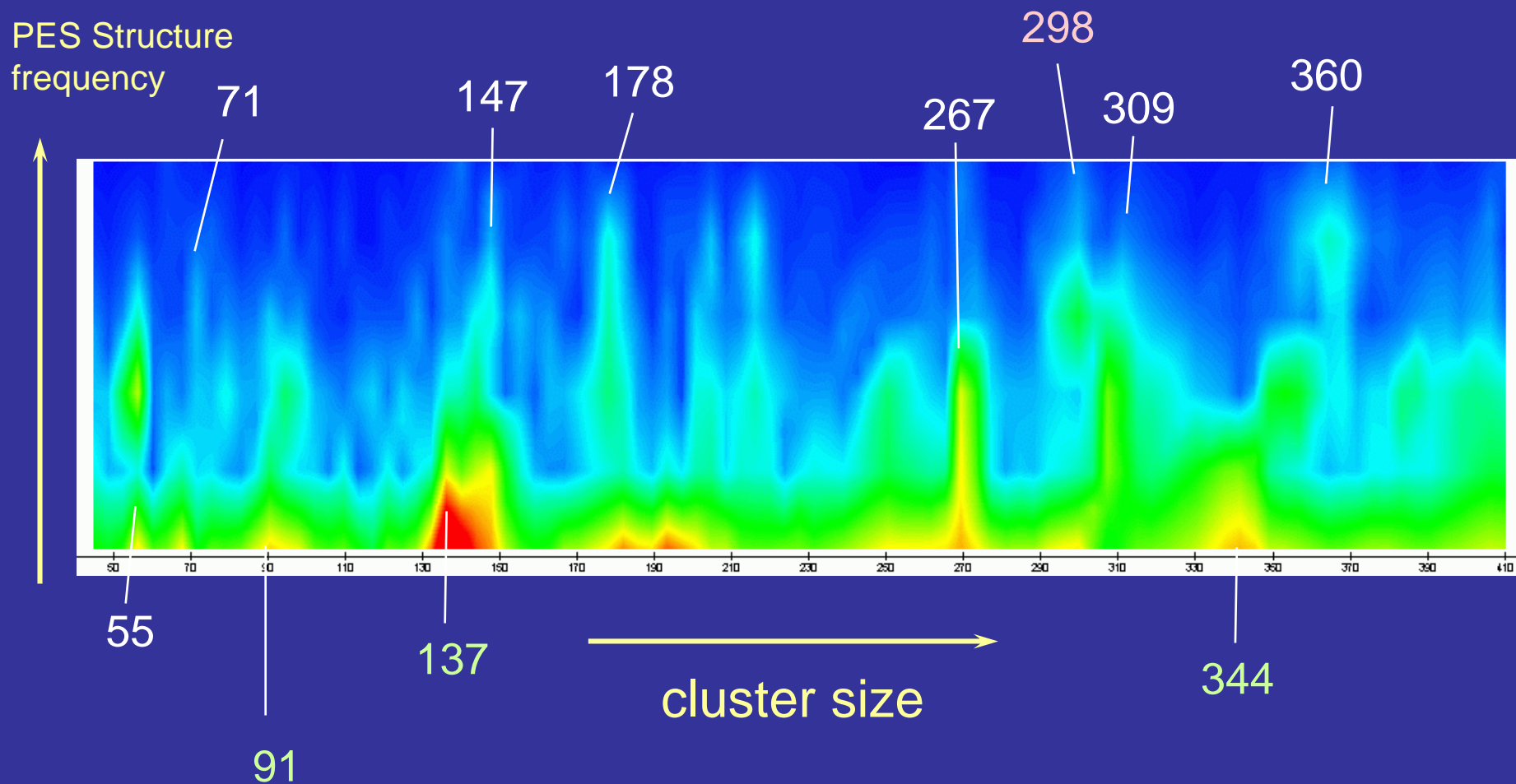
strong variation with size

**highly structured spectra  
indicate high symmetry!**



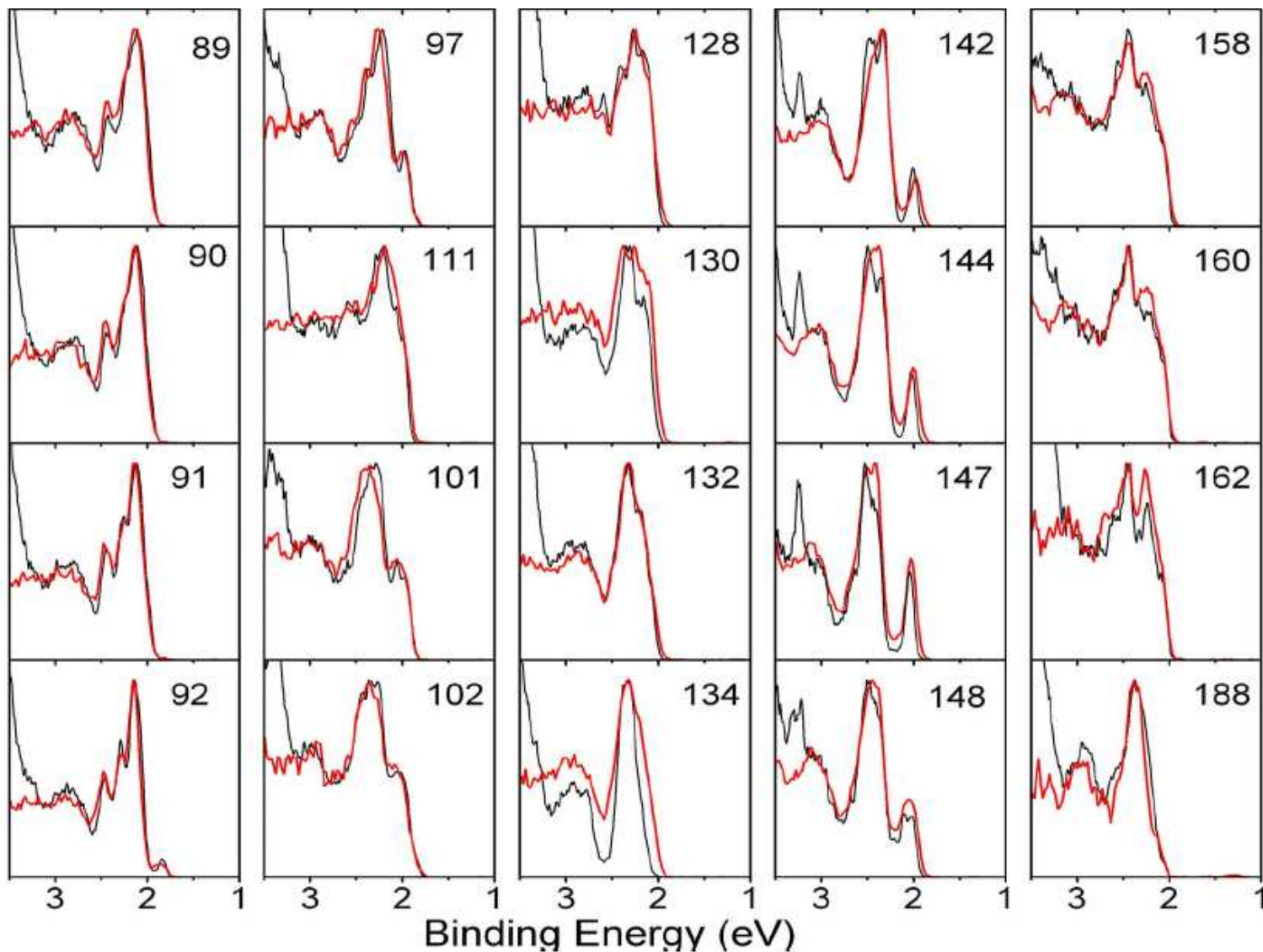


# Fourier Transform PES





# Comparison with potassium clusters



$K_n^-$

$Na_n^-$

Energy axis  
scaled by  
Fermi energy



# Program

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Photoelectron spectroscopy  
cluster thermalization

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Structure of larger clusters  
Comparison with potassium clusters

Noble metal clusters

**Electronic structure**  
**Geometrical structure**  
**special case: gold clusters**  
**Comparison Na, Cu, Ag, Au**

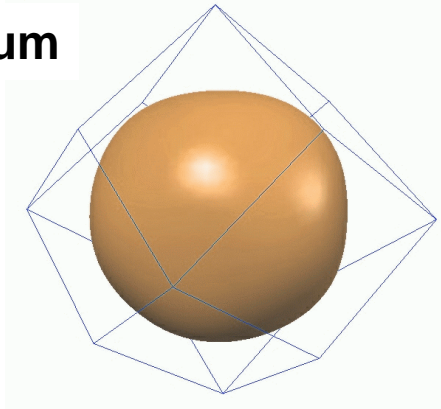
Angle resolved photoelectron spectroscopy

**Basics**  
**Results on Na, Ag, Cu**



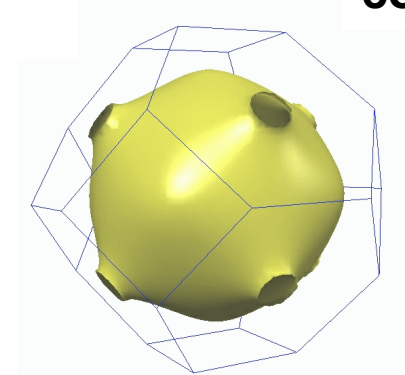
# Comparison of alkali and noble metals

sodium

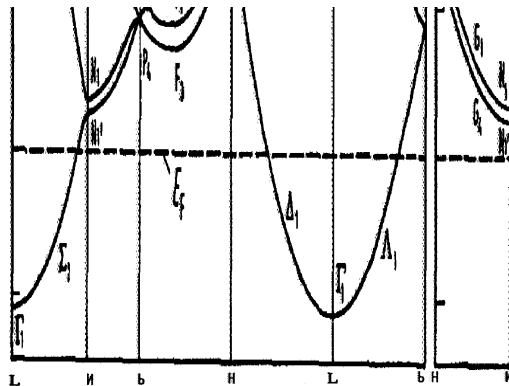


Fermi surfaces

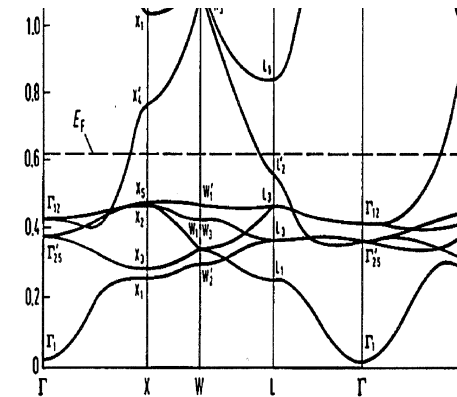
copper



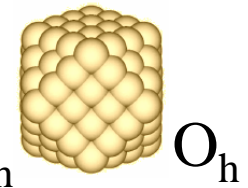
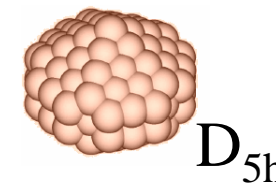
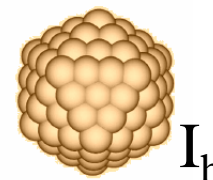
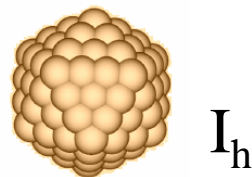
Band structures



d-Band



Predicted cluster geometries

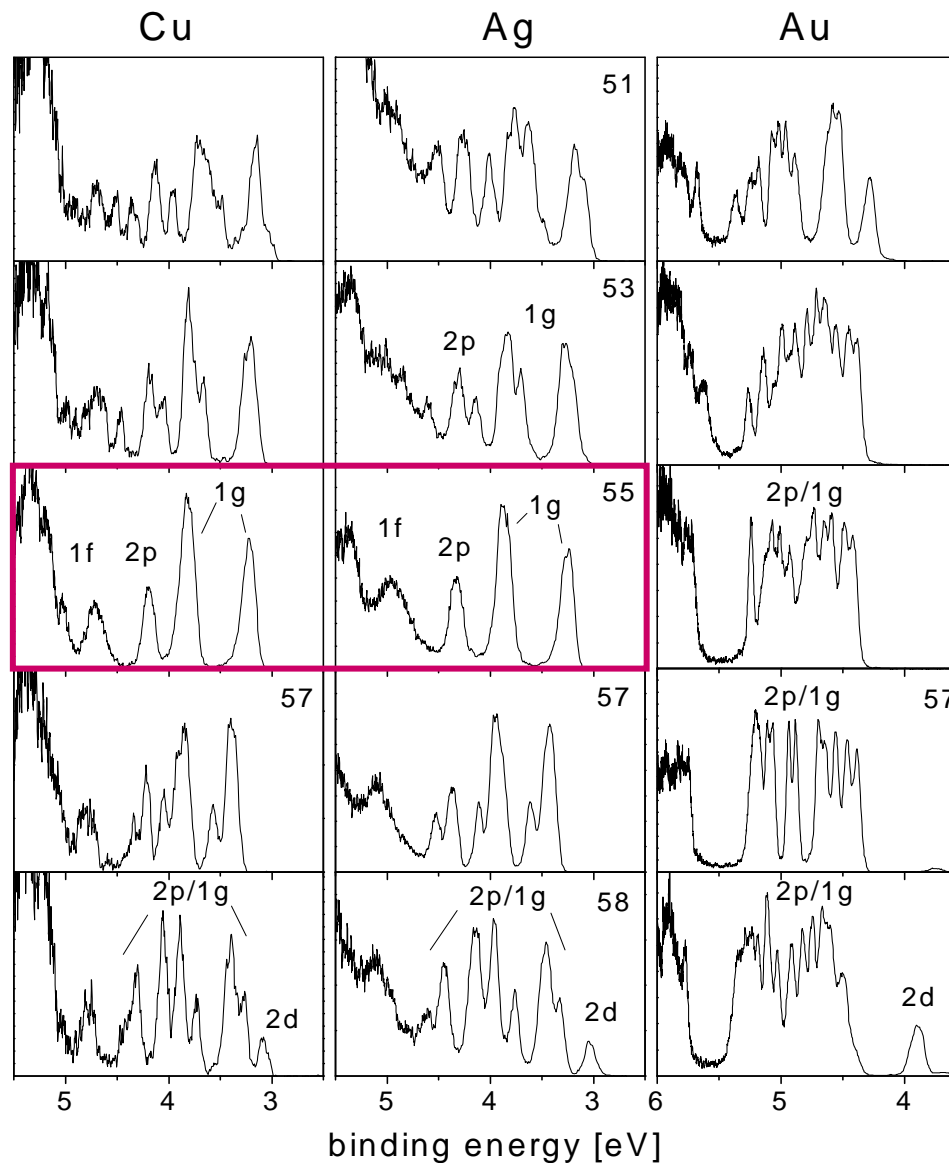




# PES of noble metal cluster anions

size 55:  
highly degenerate states  
for copper and silver!

size 58:  
appearance of a  
new shell (2d)

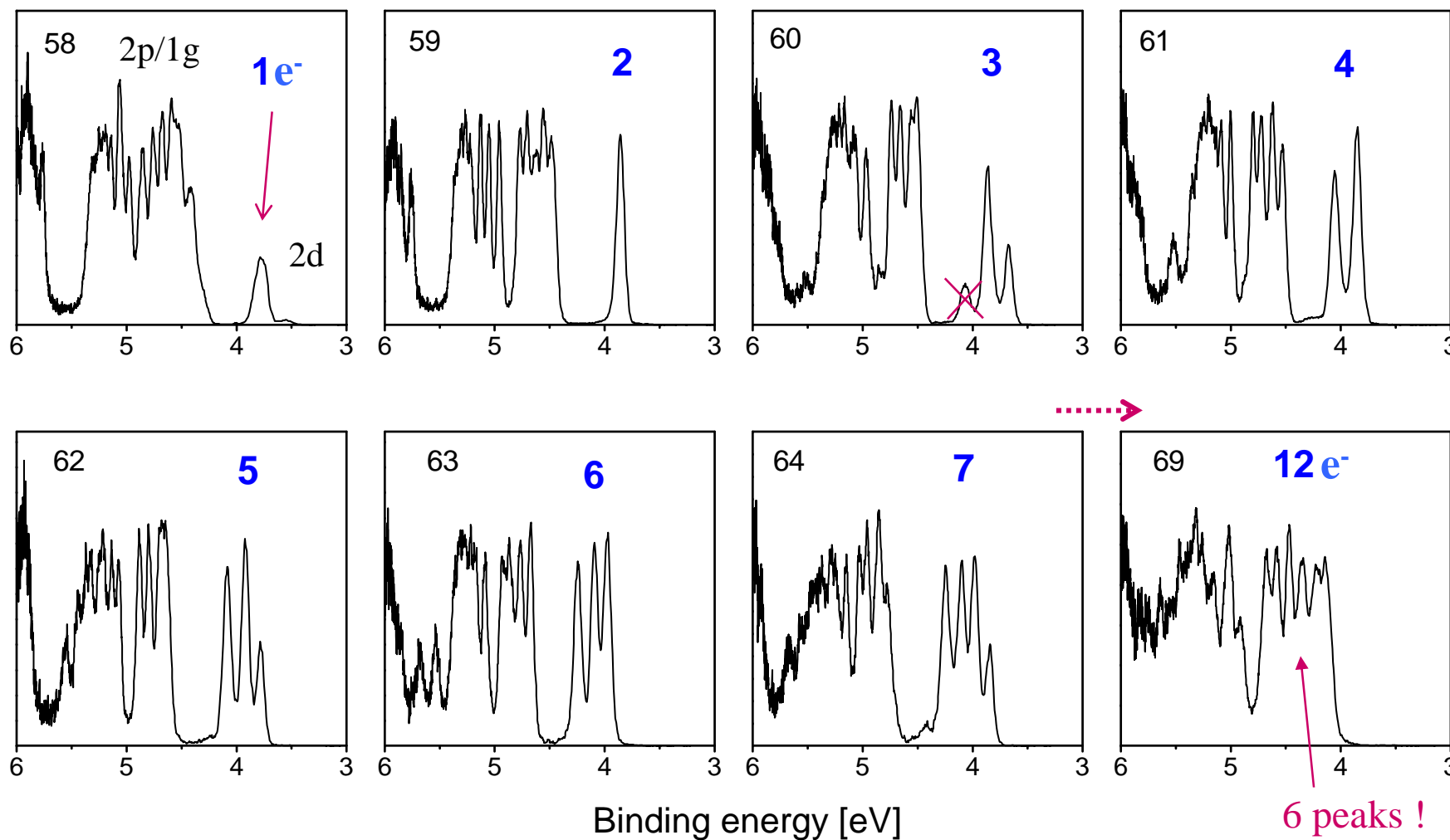






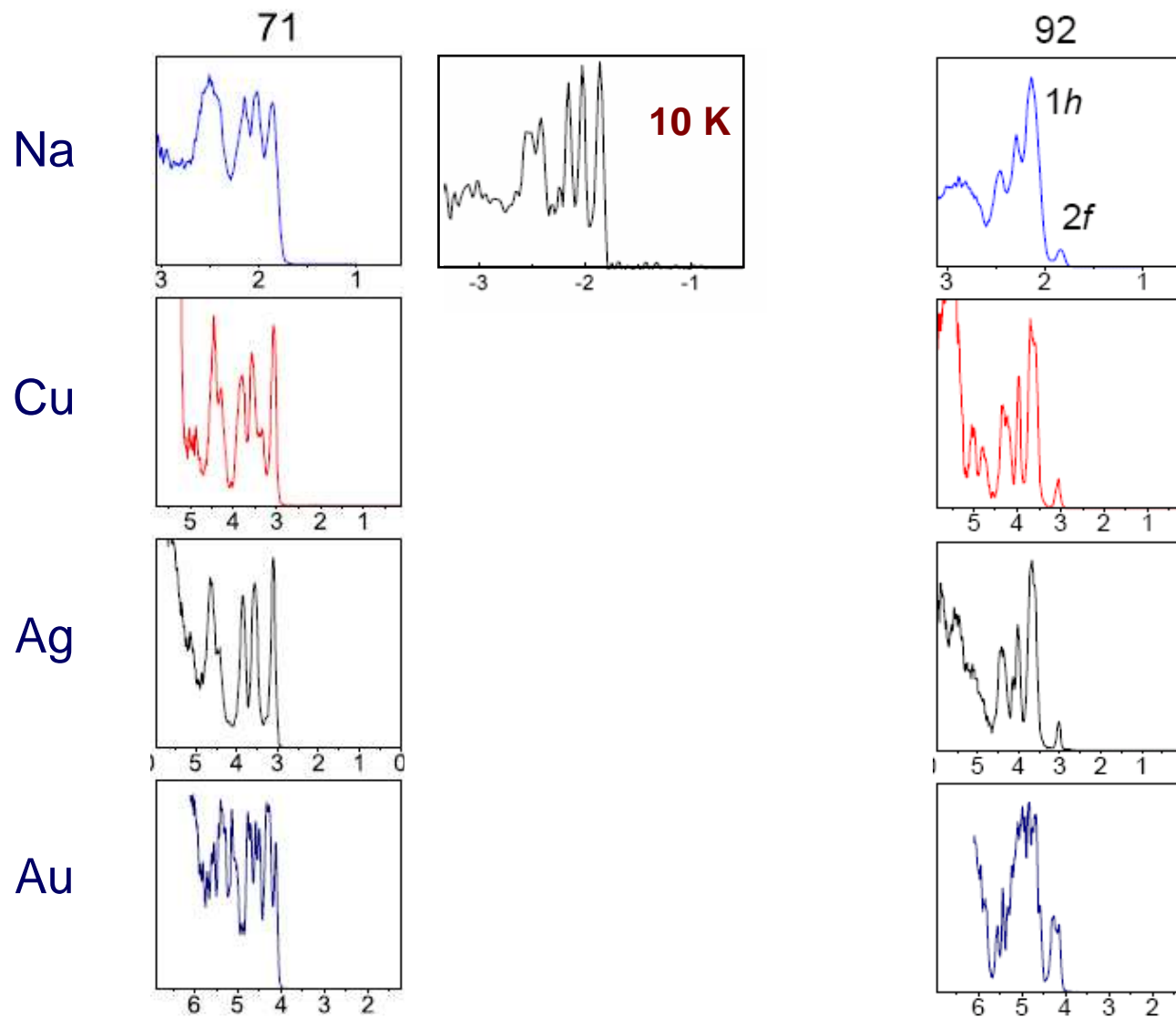
# Counting electrons: gold clusters

PES of  $Au_n^-$ ,  $n = 58-69$





# Comparison Na-Cu-Ag-Au



**Very similar !**

**Strong deviation only for gold clusters!**



# Program

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Angle resolved photoelectron spectroscopy

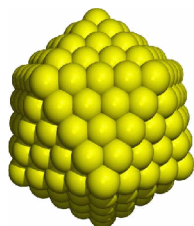
**Basics**

**Results on Na, Ag, Cu**



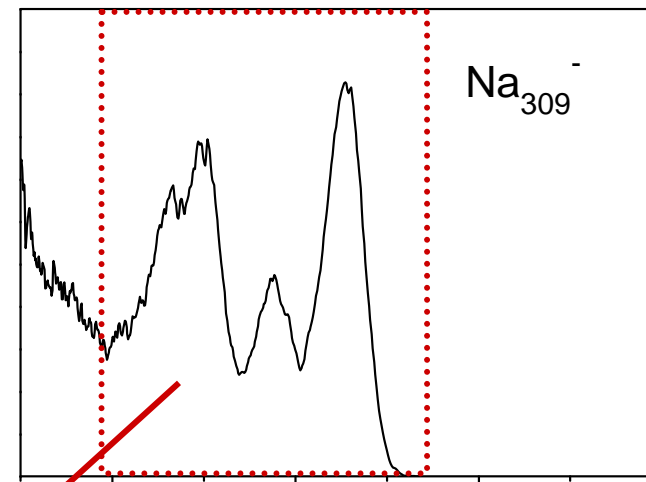
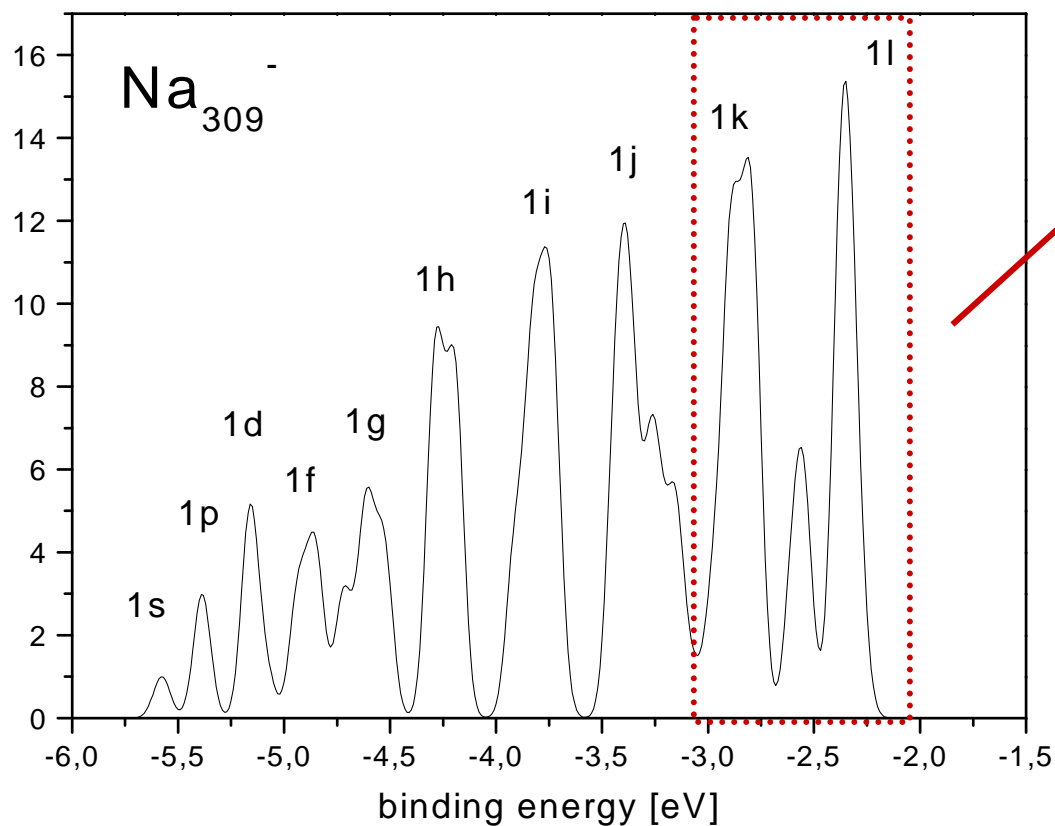
Universität Freiburg

# Electron shell structure in a large cluster



Icosahedral symmetry!

Calculated DOS



measured  
photoelectron  
spectrum

DFT- calculations by  
M. Moseler  
and B. Huber,  
Freiburg

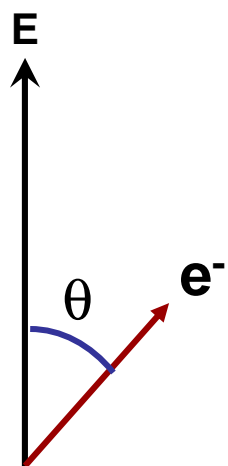


# Basics of angular resolved PES

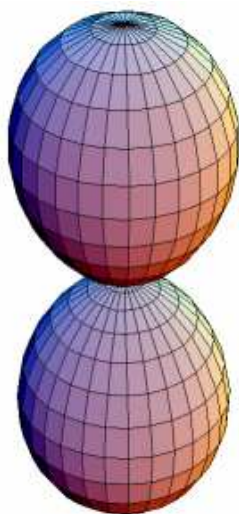
Single photon effect on atoms, molecules or clusters:  
angular distribution of photoelectrons can be described by „ $\beta$ -parameter“

$$f(\theta) = 1 + \beta \left( \frac{3}{2} \cos^2 \theta - \frac{1}{2} \right)$$

Light  
Polarization

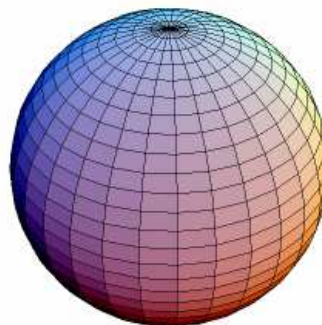


$\beta = 2$



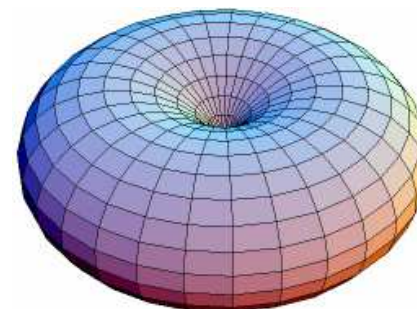
parallel

$\beta = 0$



isotropic

$\beta = -1$



perpendicular



# Cooper-Zare formula

Calculation of  $\beta$  for ionization out of an angular momentum eigenstate (averaged over  $m_l$ )

$$\beta = \frac{l(l-1)\sigma_{l-1}^2 + (l+1)(l+2)\sigma_{l+1}^2 - 6l(l+1)\sigma_{l-1}\sigma_{l+1}\cos(\delta_{l+1} - \delta_{l-1})}{(2l+1)[l\sigma_{l-1}^2 + (l+1)\sigma_{l+1}^2]}$$

$l$  : angular momentum

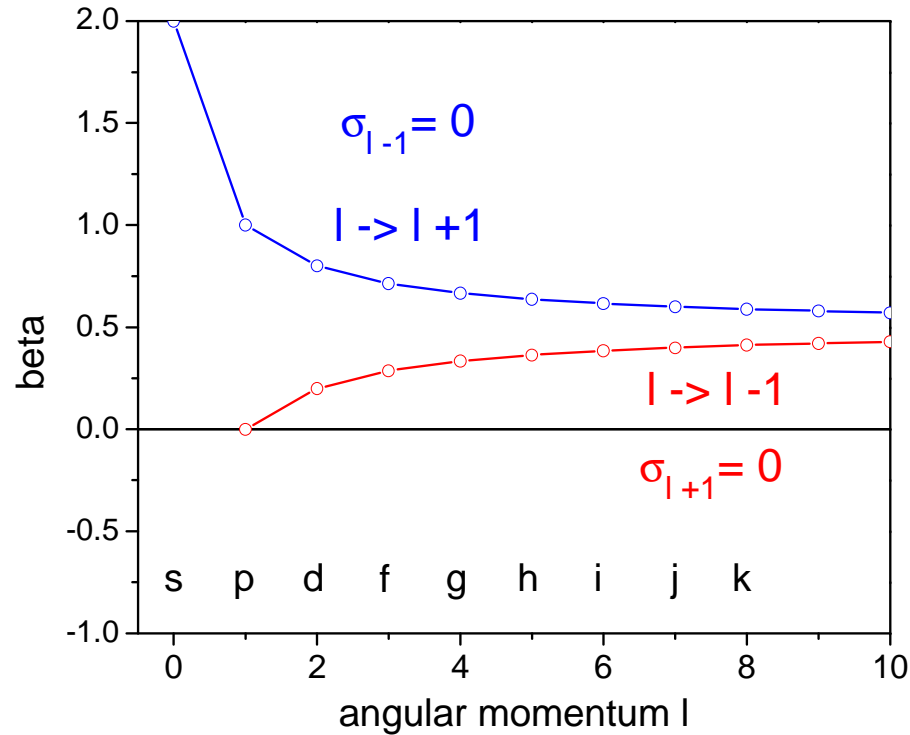
$\delta_{l\pm 1}$  : phase shift of outgoing ( $l\pm 1$ ) wave

$\sigma_{l\pm 1}$  : radial dipole matrix element

$$\sigma_{l\pm 1} = \int_0^{\infty} R_{il}(r)rR_{f(l\pm 1)}(r)dr$$



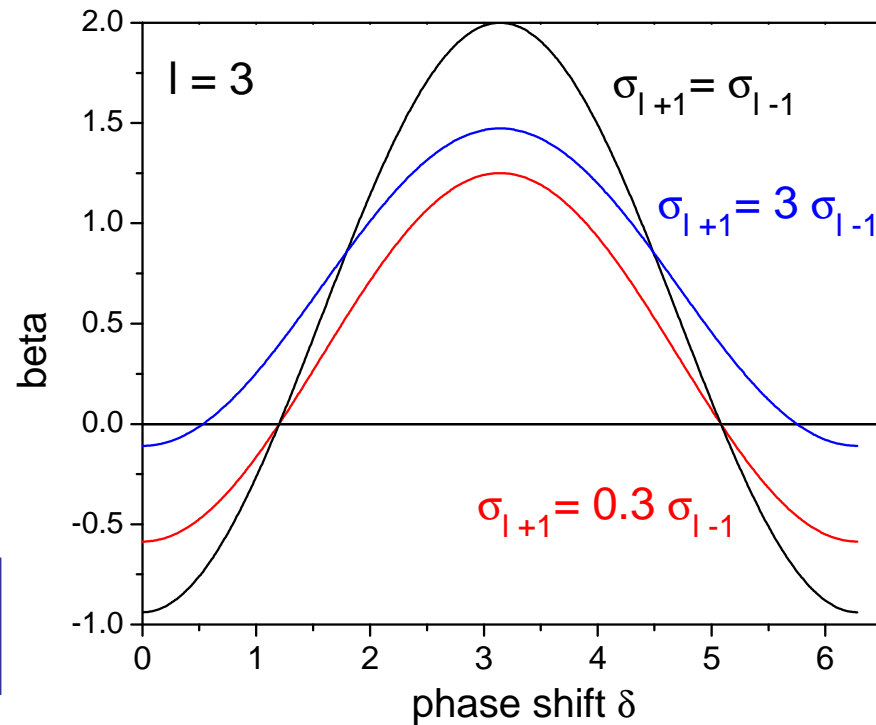
# Variation of $\beta$ with $l$ and $\delta$



Emission only into either  $l+1$  or  $l-1$  :  
 $\Rightarrow \beta$  always positive!

Negative values of  $\beta$  only if both partial waves interfere, i.e. if

$$\sigma_{l+1} \approx \sigma_{l-1} \quad \text{and} \quad \delta \approx 0$$

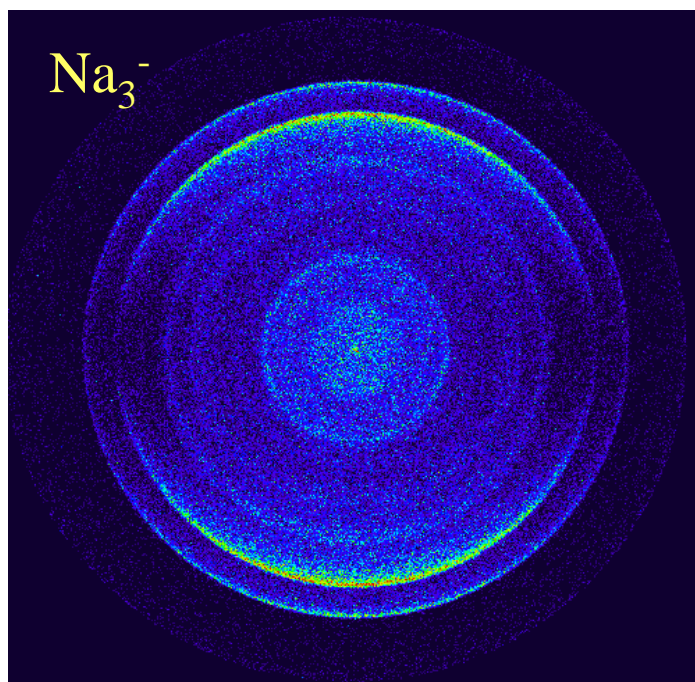
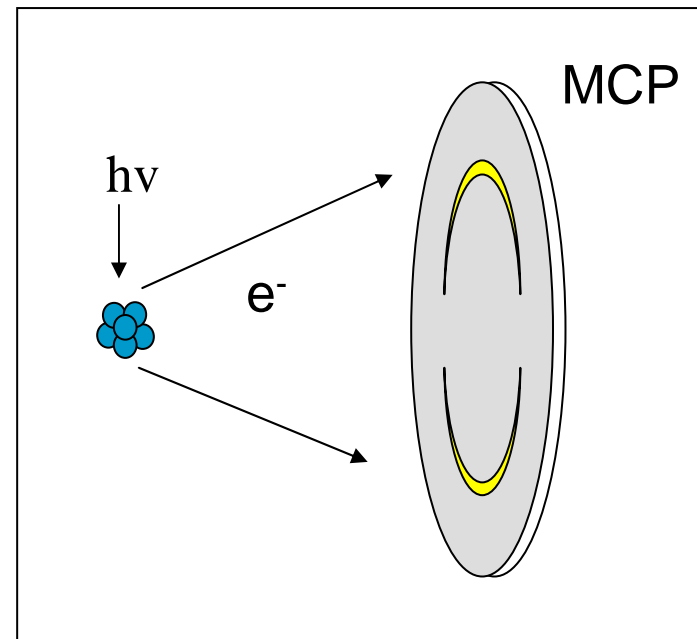




# Imaging PES: principle

Projection of emitted photoelectron onto MCP:

Measurement of angular and kinetic energy distribution



laser  
polarization

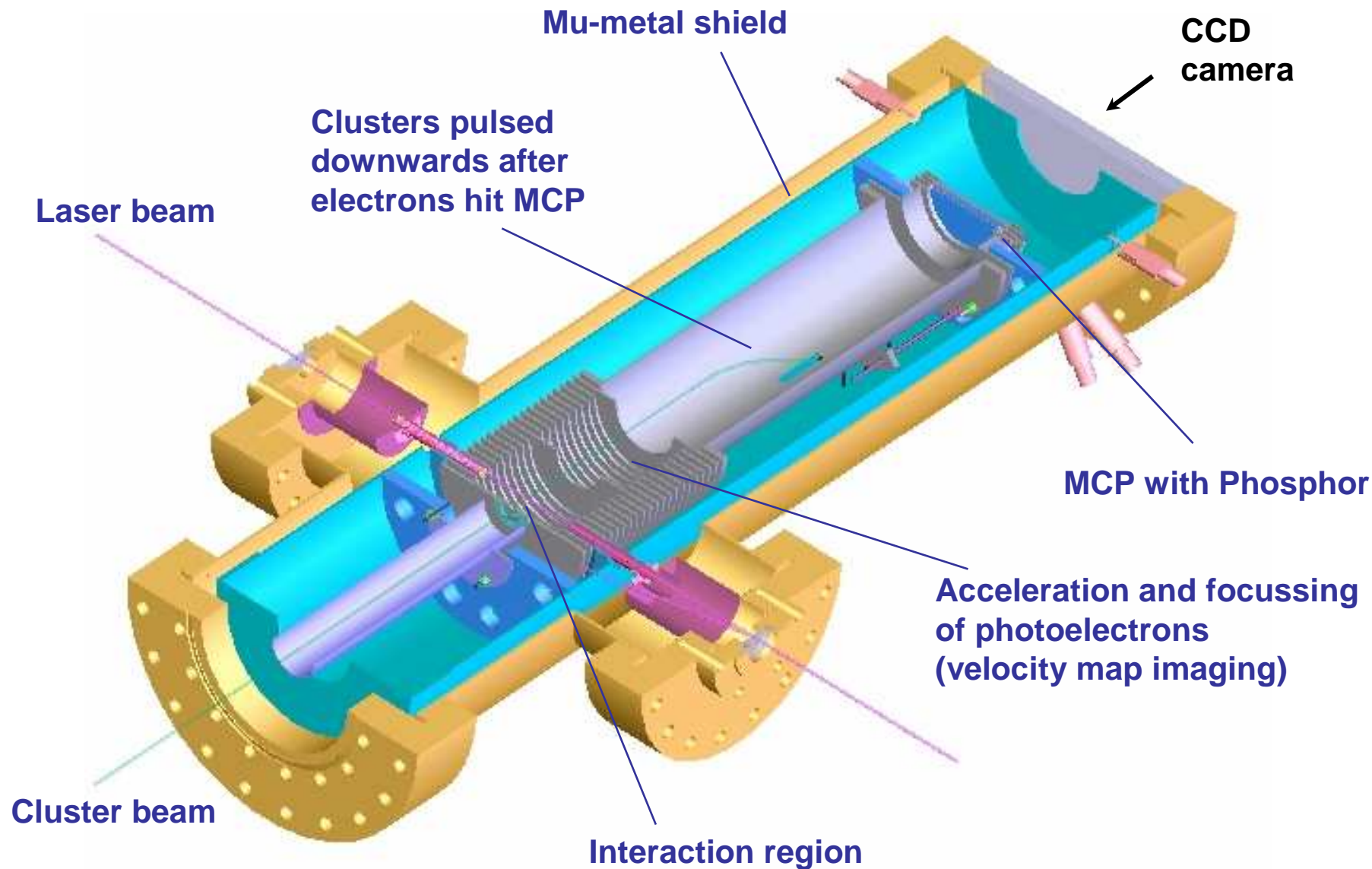
308 nm

raw data



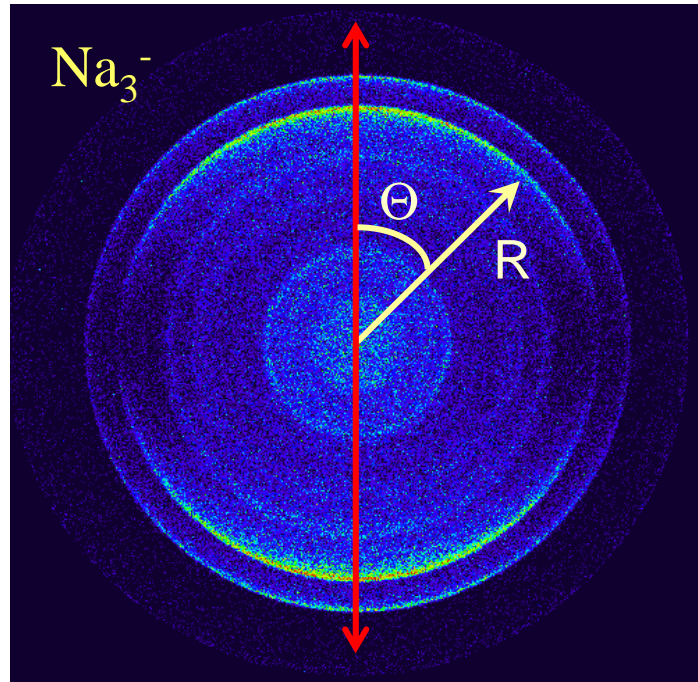


# Imaging spectrometer

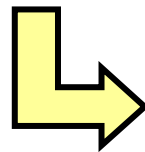




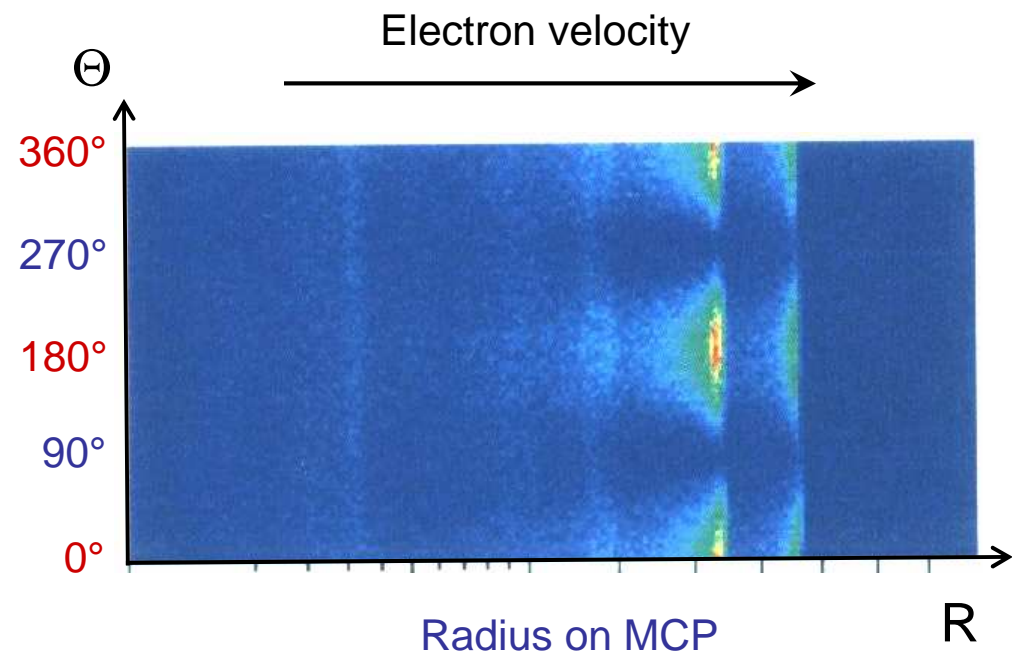
# Presentation of the results: projection



Laser polarization



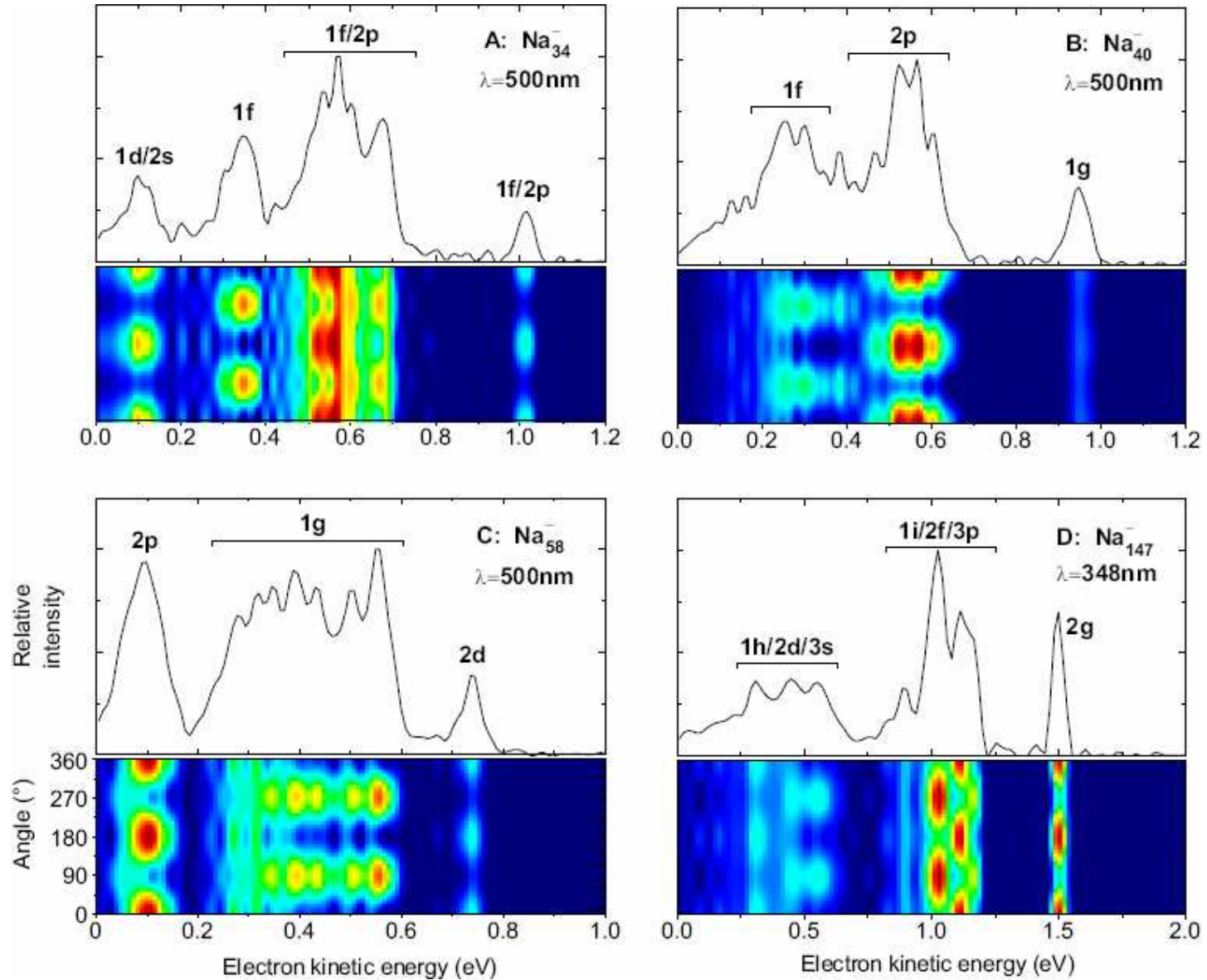
Presentation of spectra as  
( $R, \Theta$ ) - Graphs





# Angular distribution of electron shells

p-BaseX  
deconvolution

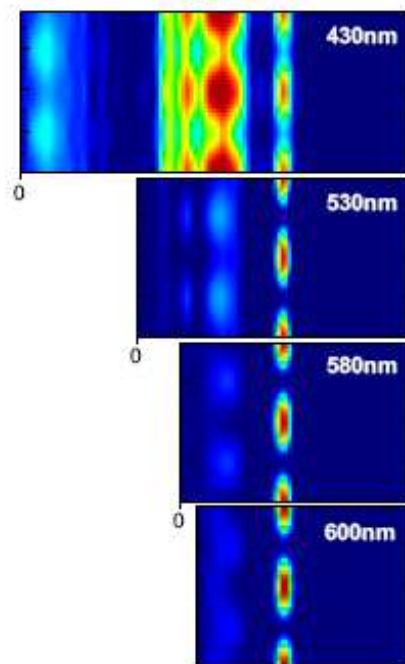
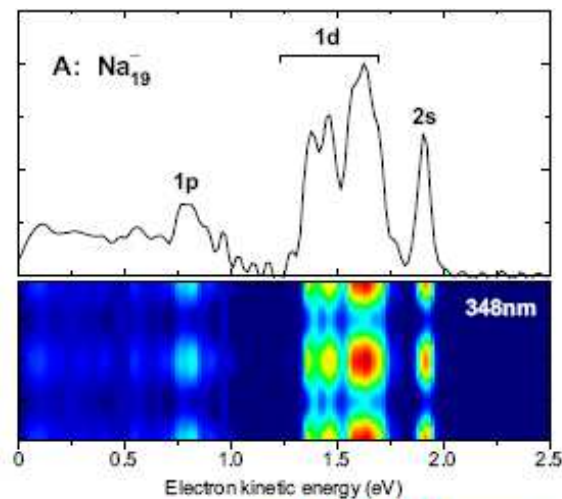




# Photon energy dependence

$\text{Na}_{19}^-$

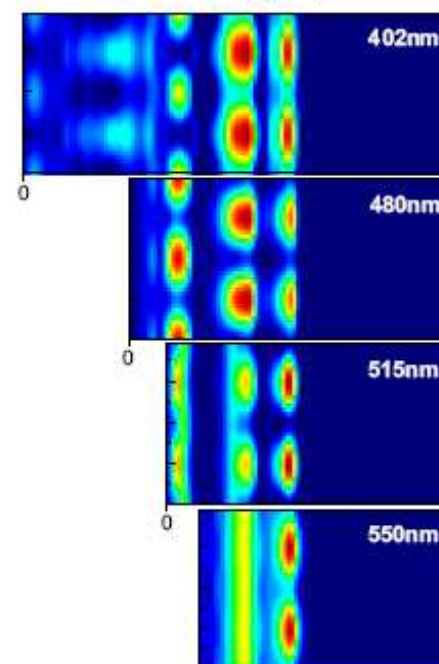
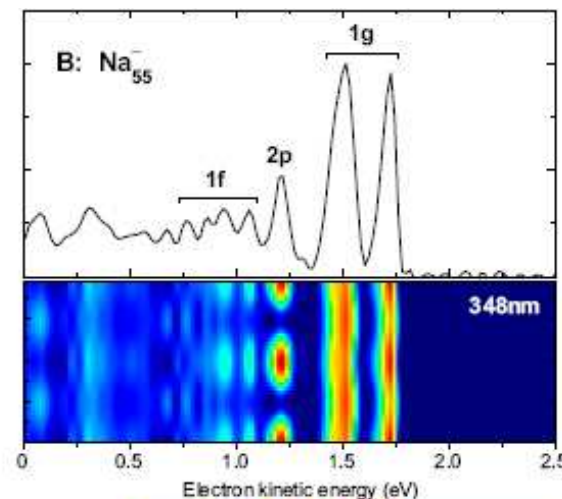
electronic  
closed shell



strong  
variations!

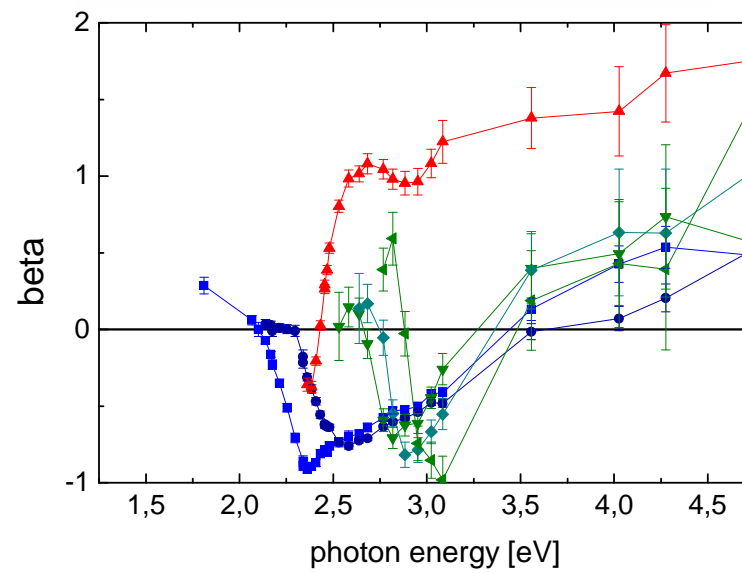
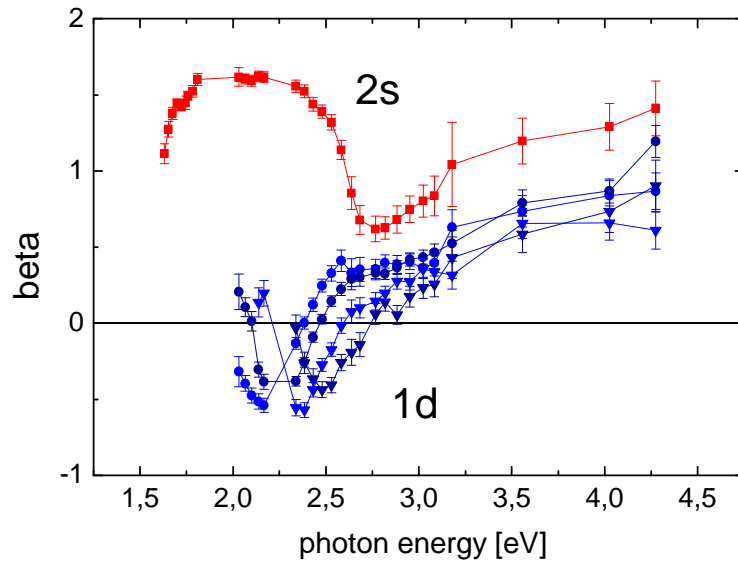
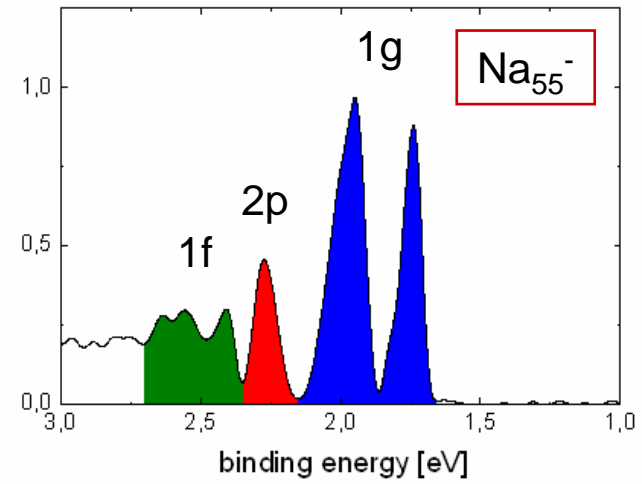
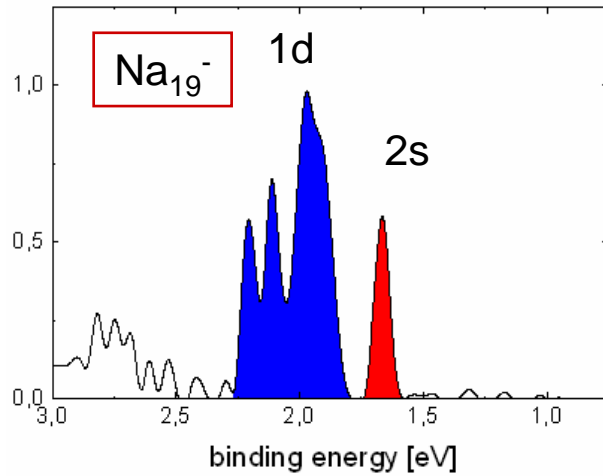
$\text{Na}_{55}^-$

atomic  
closed shell



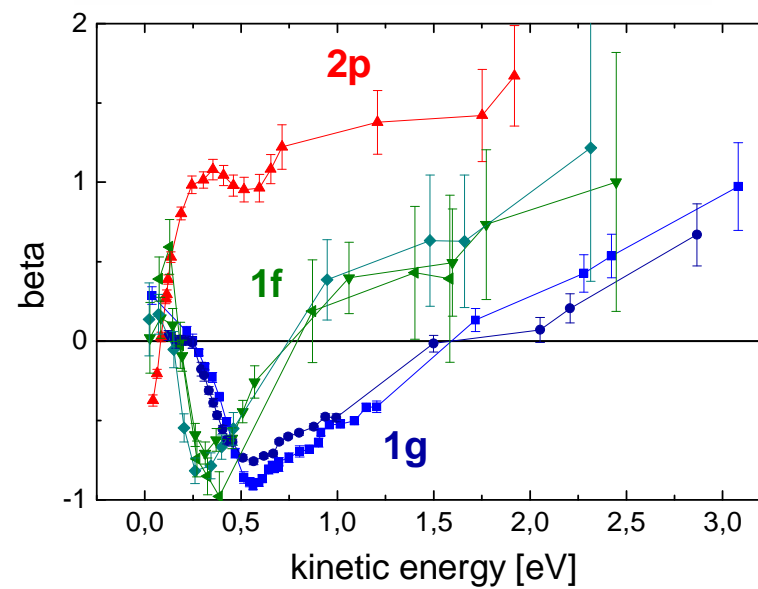
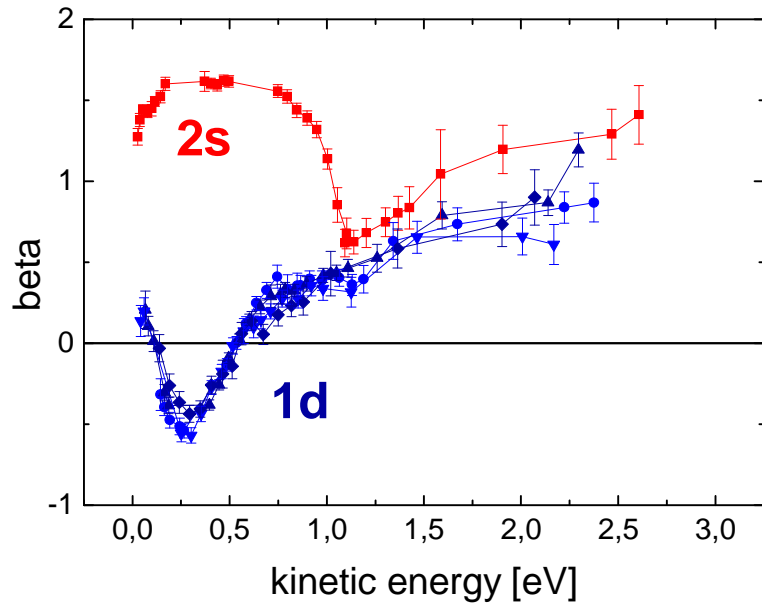
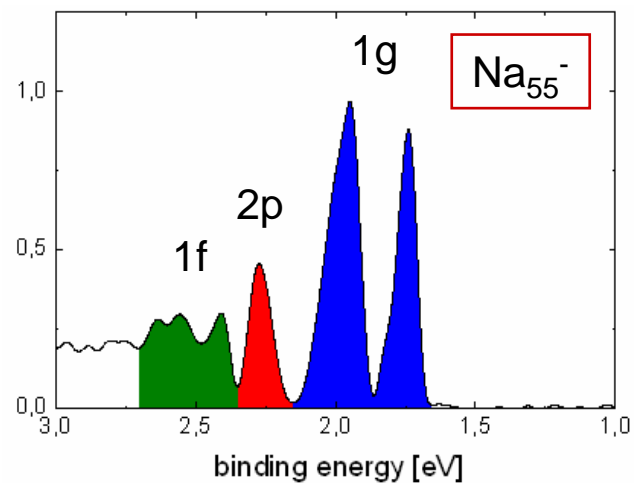
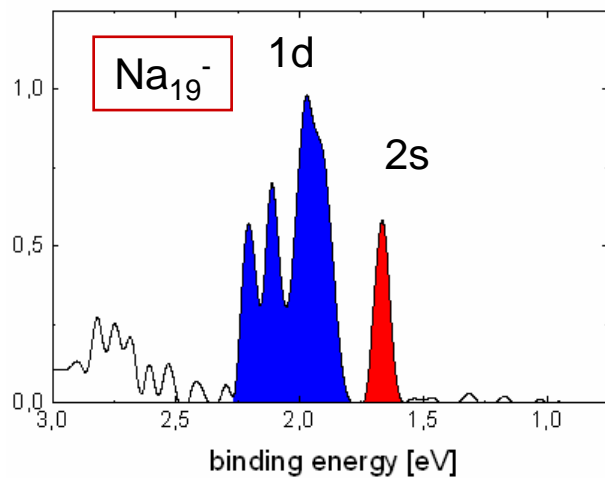


# Extracted beta parameters



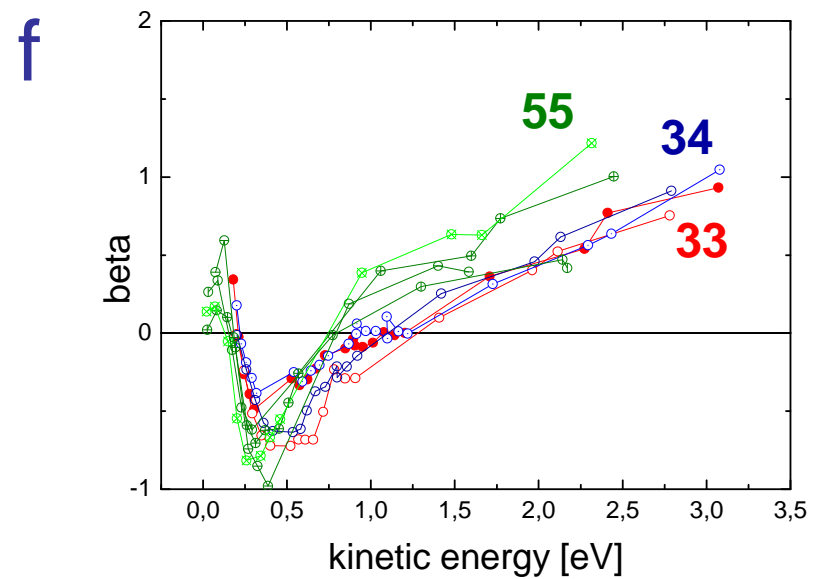
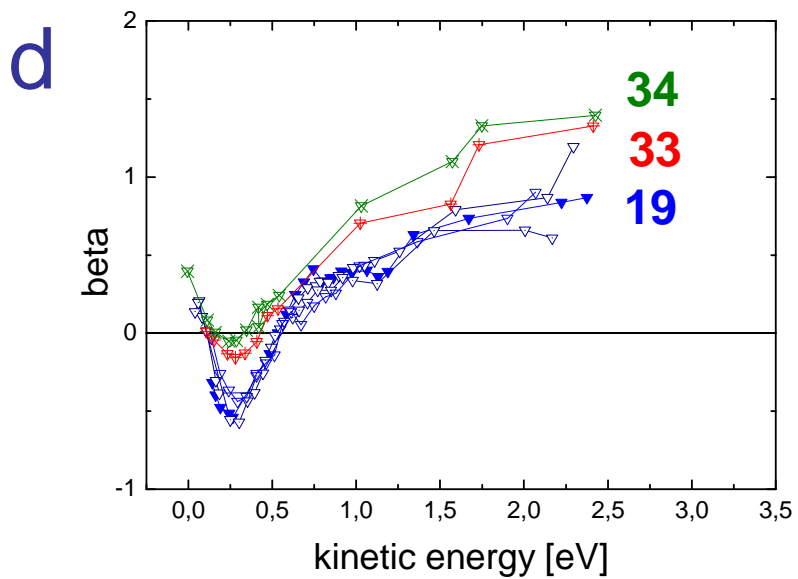
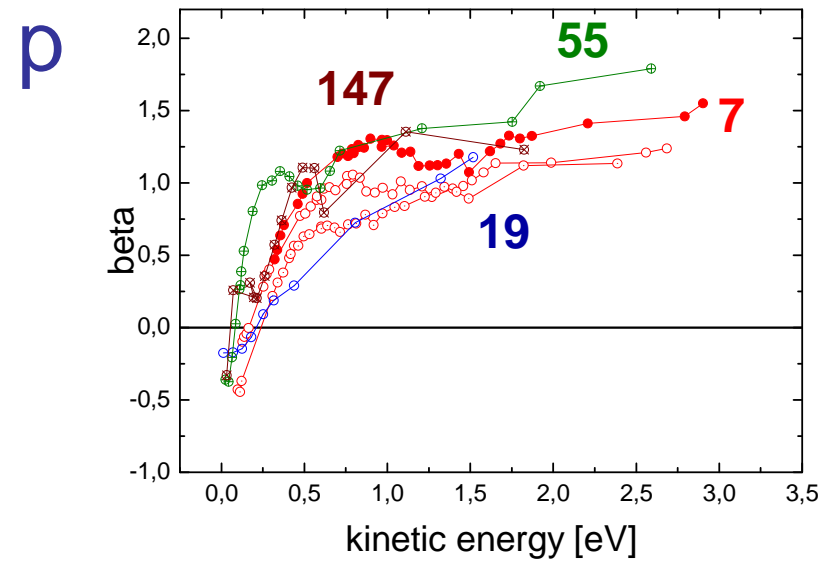
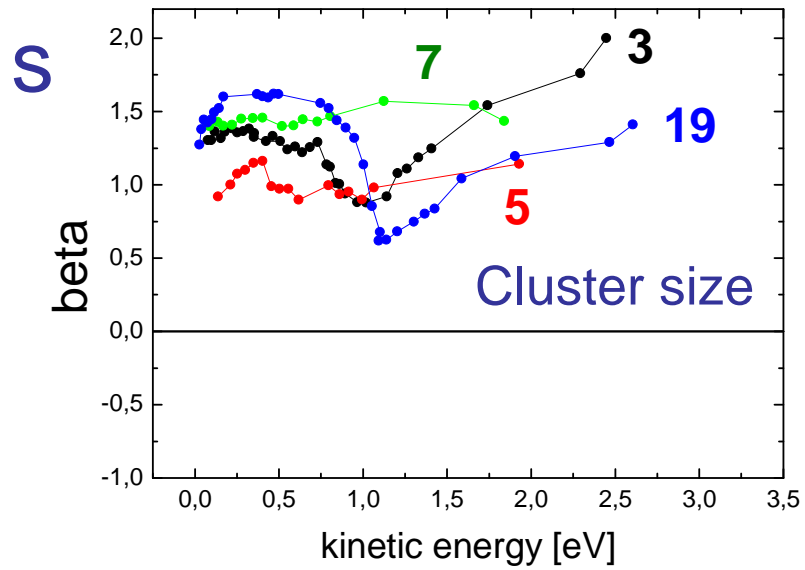


# Extracted beta parameters



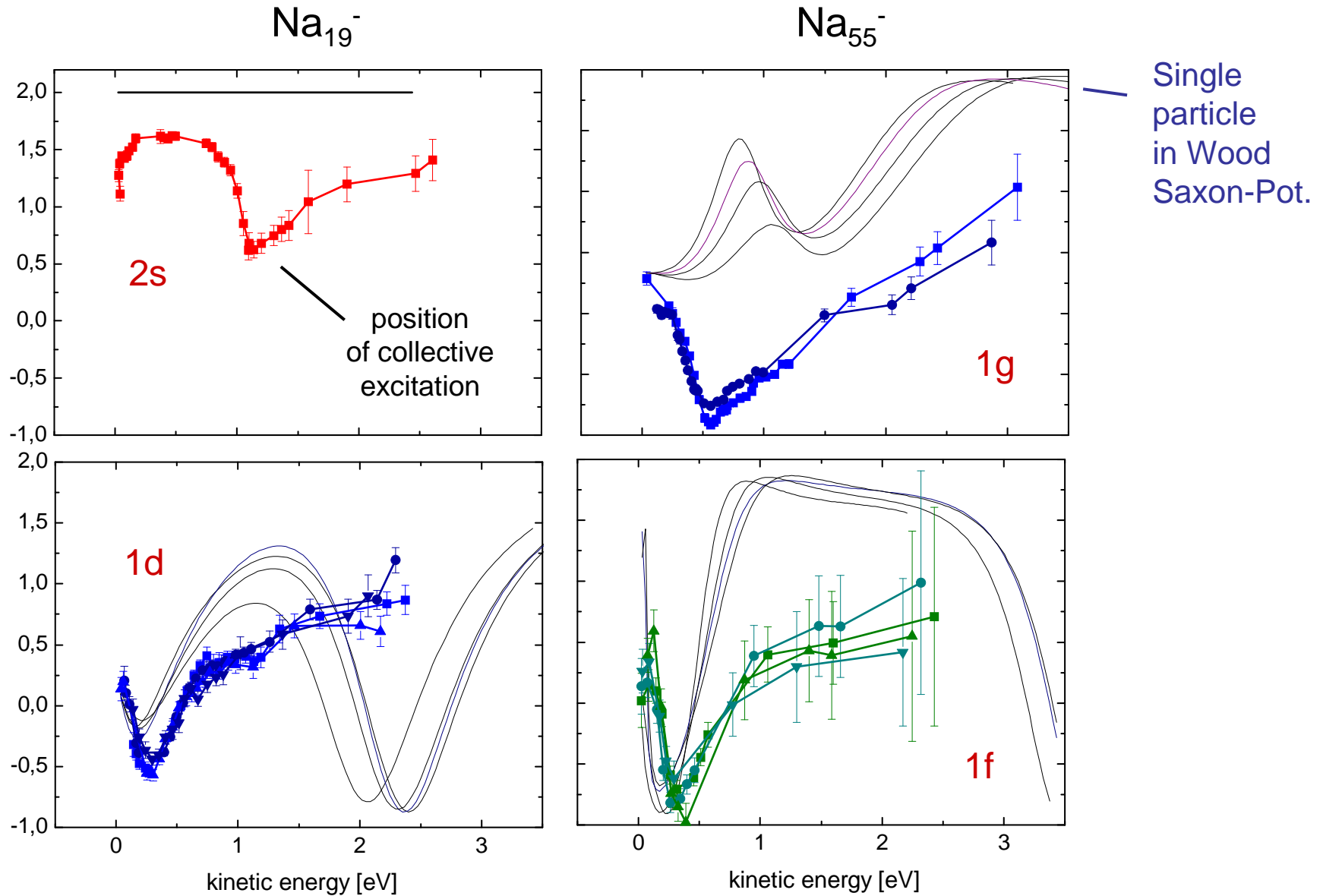


# Universal behaviour of I-states





# Comparison with model calculations

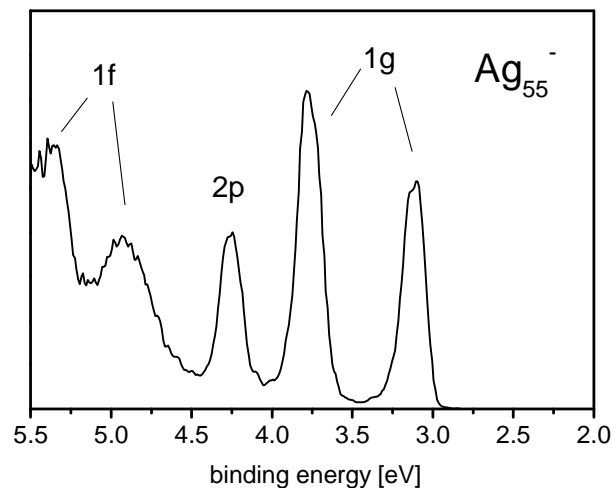






# Silver clusters: angular distributions

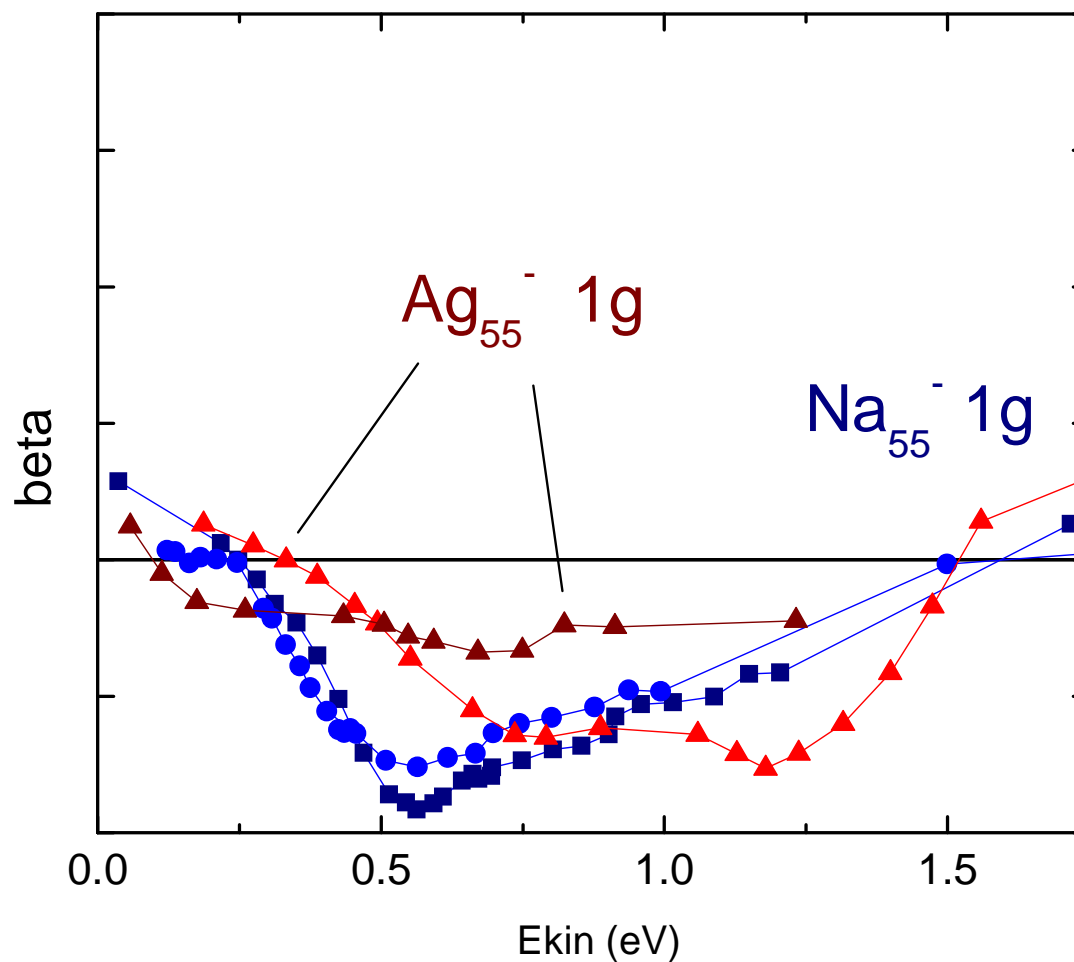
## Photoelectron spectrum



**Different behaviour  
for the two 1-g states!**

**Strong perturbation of  
s-band by hybridization  
with d-band?**

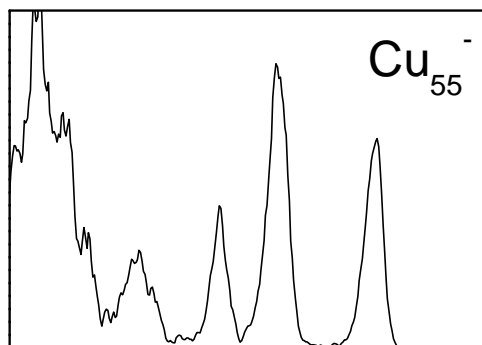
## Beta parameter





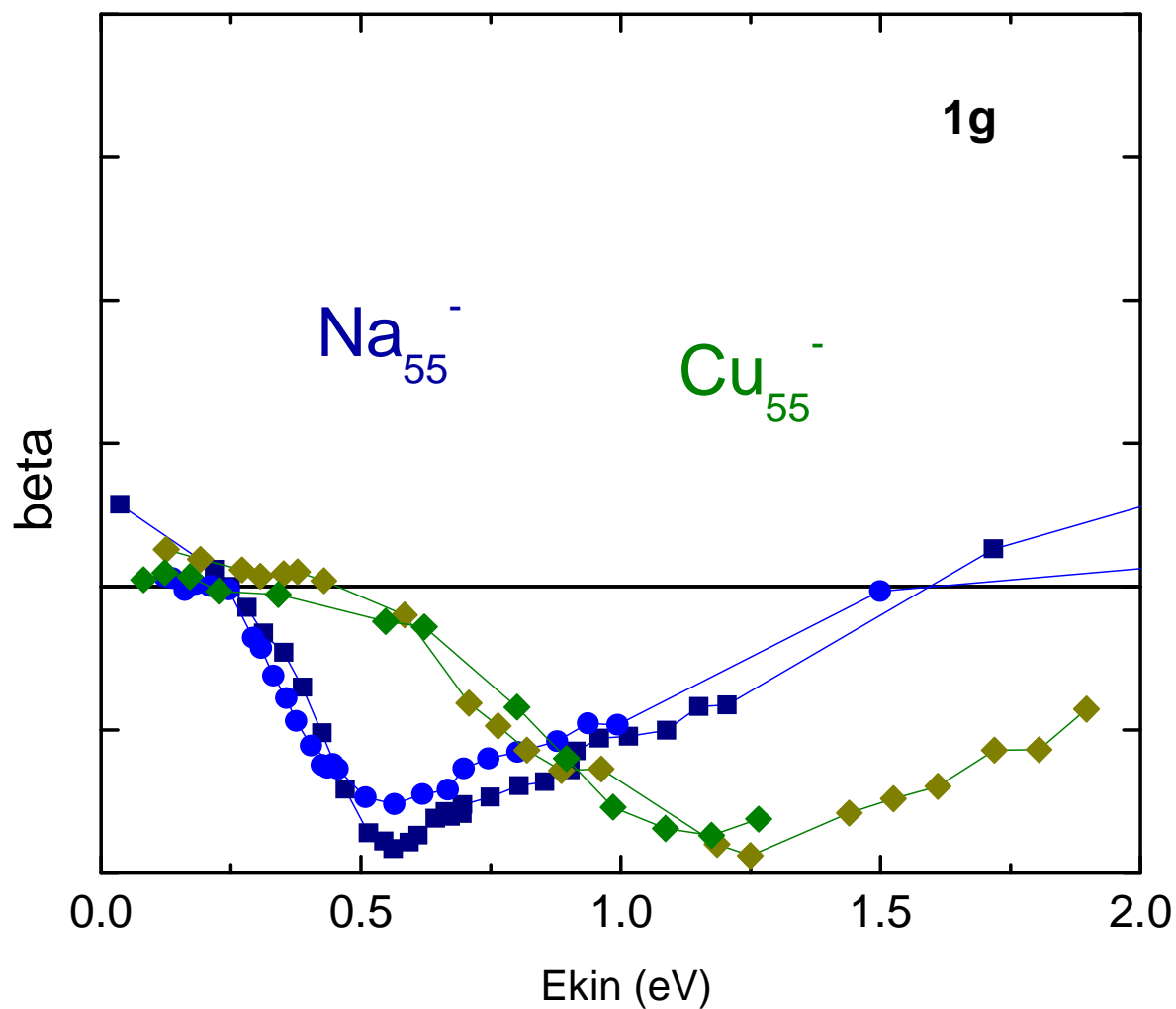
# Copper clusters: angular distributions

Photoelectron spectrum



Very similar behaviour!

Beta parameter





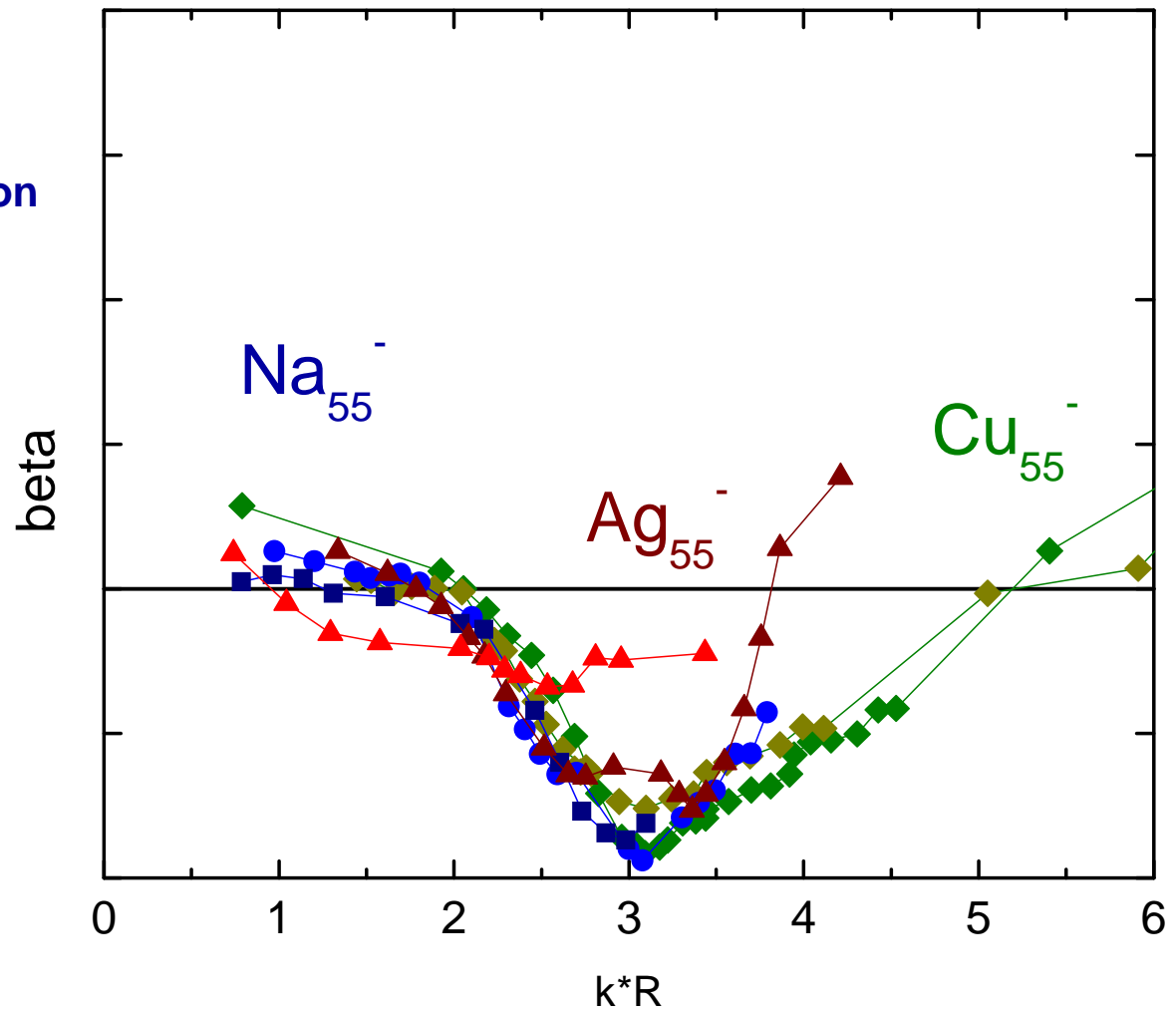
# Comparison sodium, copper, silver

Scaled to

$$k * R$$

$k$ : wavevector free electron  
 $R$ : cluster radius

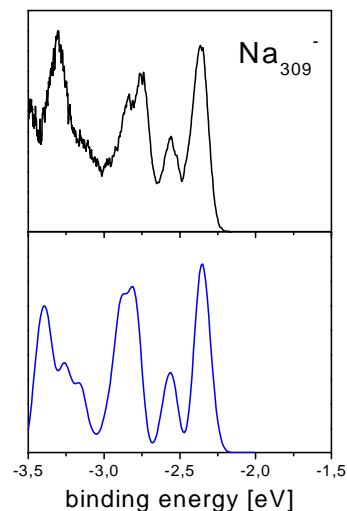
**Universal  
behaviour!**



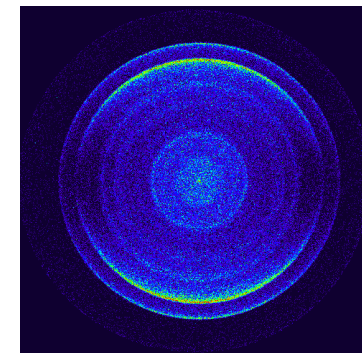


# Summary

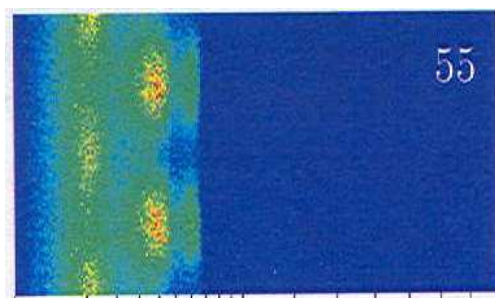
Sodium clusters:  
„perfect“ shell structure



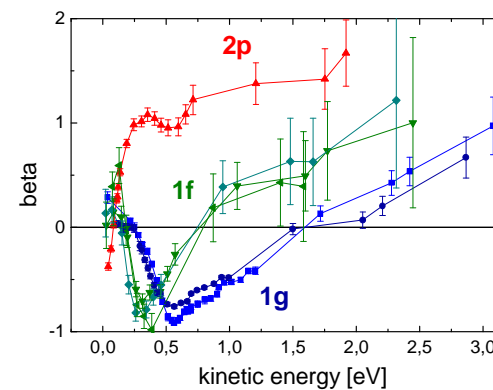
Imaging spectroscopy:  
angular resolved  
PES of clusters



Perpendicular distributions:  
indicate destructive  
interference of outgoing  
partial waves



Energy dependence:  
clear reminiscence of  
angular momentum state





# Acknowledgment

Thanks to



**Oleg Kostko:**  
PES

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ARPES

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caloric curves/  
ARPES

**Raphael Kuhnen**  
**Adam Piechaczek**  
ARPES

**Jan Huwer:** ARPES